



SQL language: basics

Nested queries

Nested queries

- Introduction
- The IN operator
- The NOT IN operator
- The tuple constructor
- The EXISTS operator
- The NOT EXISTS operator
- Correlation among queries
- The division operation
- Table functions



Nested queries

Introduction

- A nested query is a **SELECT** statement contained within another query
 - query nesting allows decomposing a complex problem into simpler subproblems
- **SELECT** statements may be introduced
 - within a predicate in the **WHERE** clause
 - within a predicate in the **HAVING** clause
 - in the **FROM** clause

Supplier and part DB (1/2)

- P (PId, PName, Color, Size, Store)
- S (SId, SName, #Employees, City)
- SP (SId, PId, Qty)

Supplier and part DB (1/2)

P

<u>PId</u>	<u>PName</u>	<u>Color</u>	<u>Size</u>	<u>Store</u>
P1	Jumper	Red	40	London
P2	Jeans	Green	48	Paris
P3	Blouse	Blue	48	Rome
P4	Blouse	Red	44	London
P5	Skirt	Blue	40	Paris
P6	Shorts	Red	42	London

SP

<u>SId</u>	<u>PId</u>	<u>Qty</u>
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

S

<u>SId</u>	<u>SName</u>	<u>#Employees</u>	<u>City</u>
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

Nested queries (no.1)


- Find the codes of the suppliers that are based in the same city as S1

- By using a formulation with nested queries, the problem may be decomposed into two subproblems
 - city of supplier S1
 - codes of the suppliers based in the same city

Nested queries (no.1)

- Find the codes of the suppliers that are based in the same city as S1

```
SELECT SId
FROM S
WHERE City = (SELECT City
              FROM S
              WHERE SId='S1');
```



- The '=' operator may be used only if it is known in advance that the inner SELECT statement always returns a single value

Equivalent formulation (no.1)

- Find the codes of the suppliers that are based in the same city as S1
- An equivalent formulation may be defined using a join operation

Equivalent formulation

- The equivalent formulation with join is characterized by
- a FROM clause including the tables referenced by the FROM clauses of each SELECT statement
 - appropriate join conditions in the WHERE clause
 - possible selection predicates added in the WHERE clause

FROM clause (no.1)

➤ Find the codes of the suppliers that are based in the same city as S1

```
SELECT SId
FROM (S) ← SX
WHERE City = (SELECT City
              FROM (S) ← SY
              WHERE SId='S1');
```

FROM clause (no.1)

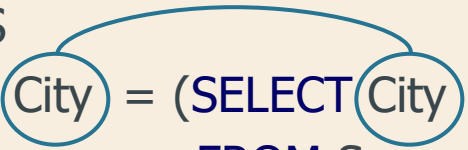
- Find the codes of the suppliers that are based in the same city as S1

```
SELECT ...  
FROM S AS SX, S AS SY  
...
```

Join condition (no.1)

- Find the codes of the suppliers that are based in the same city as S1

```
SELECT SId
FROM S
WHERE City = (SELECT City
               FROM S
               WHERE SId='S1');
```

A blue curved line connects the 'City' column in the outer query's WHERE clause to the 'City' column in the subquery's WHERE clause, indicating the join condition.

Join condition (no.1)

- Find the codes of the suppliers that are based in the same city as S1

```
SELECT ...  
FROM S AS SX, S AS SY  
WHERE SX.City=SY.City  
...
```


Selection predicate (no.1)

- Find the codes of the suppliers that are based in the same city as S1

```
SELECT SId
FROM S
WHERE City = (SELECT City
              FROM S
              WHERE SId='S1');
```

SELECT clause (no.1)

➤ Find the codes of the suppliers that are based in the same city as S1

```
SELECT SY.SId
FROM S AS SX, S AS SY
WHERE SX.City=SY.City AND
      SX.SId='S1';
```

Equivalent formulation (no.2)

- Find the codes of the suppliers whose number of employees is smaller than the maximum number of employees

```
SELECT SId
FROM S
WHERE #Employees < (SELECT MAX(#Employees)
                     FROM S);
```

- Is it possible to define an equivalent formulation with join?

Equivalent formulation (no.2)

- Find the codes of the suppliers whose number of employees is smaller than the maximum number of employees

```
SELECT SId
FROM S
WHERE #Employees < (SELECT MAX(#Employees)
                     FROM S);
```

- An equivalent formulation with join is not possible



Nested queries

The IN operator

The IN operator (no.1)

- Find the names of the suppliers that provide product P2

- Decomposition of the problem into two subproblems
 - codes of the suppliers of product P2
 - names of the suppliers with such codes

The IN operator (no.1)

➤ Find the names of the suppliers that provide product P2

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400



<u>SId</u>
S1
S2
S3

```
(SELECT SId  
FROM SP  
WHERE PId='P2')
```

*Codes
of the
suppliers
of P2*


The IN operator (no.1)

➤ Find the names of the suppliers that provide product P2

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId='P2')
```

The IN operator (no.1)

➤ Find the names of the suppliers that provide product P2


```
SELECT SName
FROM S
WHERE SId  (SELECT SId
      FROM SP
      WHERE PId='P2')
```

The IN operator (no.1)

➤ Find the names of the suppliers that provide product P2

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId='P2');
```

Set membership



The IN operator

- It expresses the concept of membership to a set of values
 - *AttributeName* IN (*NestedQuery*)

- It allows writing a query by
 - decomposing the problem into subproblems
 - following a “bottom-up” procedure

Equivalent formulation

- The equivalent formulation with join is characterized by
- a FROM clause including the tables referenced by the FROM clauses of each SELECT statement
 - appropriate join conditions in the WHERE clause
 - possible selection predicates added in the WHERE clause

The IN operator (no.1)

➤ Find the names of the suppliers that provide product P2

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId='P2');
```

Equivalent formulation (no.1)

➤ Find the names of the suppliers that provide product P2

```
SELECT SName
FROM S, SP
WHERE S.SId=SP.SId
      AND PId='P2';
```

The IN operator (no.2)

- Find the names of the suppliers that supply at least one red product

- Decomposition of the problem into subproblems
 - codes of the red products
 - codes of the suppliers of such products
 - names of the suppliers with such codes

The IN operator (no.2)

- Find the names of the suppliers that supply at least one red product

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId IN (SELECT PId
                           FROM P
                           WHERE Color='Red'));
```

Equivalent formulation (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId IN (SELECT PId
                           FROM P
                           WHERE Color='Red'));
```

FROM clause (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT SName
FROM (S)
WHERE SId IN (SELECT SId
              FROM (SP)
              WHERE PId IN (SELECT PId
                          FROM (P)
                          WHERE Color='Red')));
```


FROM clause (no.2)

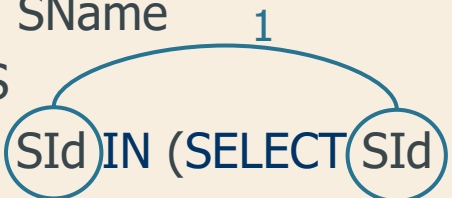
➤ Find the names of the suppliers that supply at least one red product

```
SELECT ...  
FROM S, SP, P  
...
```

Join conditions (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId IN (SELECT PId
                           FROM P
                           WHERE Color='Red')));
```



Join conditions (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT ...  
FROM S, SP, P  
WHERE S.SId=SP.SId
```

1

Join conditions (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT SName
```

```
FROM S
```

```
WHERE SId IN (SELECT SId
```

```
FROM SP
```

```
WHERE PId IN (SELECT PId
```

```
FROM P
```

```
WHERE Color='Red'));
```

2



Join conditions (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT ...  
FROM S, SP, P  
WHERE S.SId=SP.SId AND  
       SP.CodP=S.CodP  
...
```

2

Selection predicate (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId IN (SELECT PId
                           FROM P
                           WHERE Color='Red'));
```

SELECT clause (no.2)

➤ Find the names of the suppliers that supply at least one red product

```
SELECT DISTINCT SName  
FROM S, SP, P  
WHERE S.SId=SP.SId AND  
       SP.PId=P.PId AND  
       Color='Red';
```

A complex example (no.3)

➤ Find the names of the suppliers that supply at least one product supplied by suppliers of red products

P

<u>PId</u>	PName	Color	Size	Store
P1	Jumper	Red	40	London
P2	Jeans	Green	48	Paris
P3	Blouse	Blue	48	Rome
P4	Blouse	Red	44	London
P5	Skirt	Blue	40	Paris
P6	Shorts	Red	42	London

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

A complex example (no.3)

- Find the names of the suppliers that supply at least one product supplied by suppliers of red products



A complex example (no.3)

- Find the names of the suppliers that supply at least one product supplied by suppliers of red products
- The formulation with join is awkward
 - it is easier to decompose the problem into subproblems through nested queries

A complex example (no.3)

- Find the names of the suppliers that supply at least one product supplied by suppliers of red products

*Codes of the
red products*

```
SELECT PId  
FROM P  
WHERE Color='Red'
```

A complex example (no.3)

- Find the names of the suppliers that supply at least one product supplied by suppliers of red products

```
SELECT SId
FROM SP
WHERE PId IN
    (SELECT PId
     FROM P
     WHERE Color='Red')
```

*Codes of the suppliers
of red products*

A complex example (no.3)

➤ Find the names of the suppliers that supply at least one product supplied by suppliers of red products

Codes of the products supplied by suppliers of red products

```
SELECT PId
FROM SP
WHERE SId IN
    (SELECT SId
     FROM SP
     WHERE PId IN
         (SELECT PId
          FROM P
          WHERE Color='Red'))
```

A complex example (no.3)

```
SELECT SId
FROM SP
WHERE PId IN
    (SELECT PId
     FROM SP
     WHERE SId IN
         (SELECT SId
          FROM SP
          WHERE PId IN
              (SELECT PId
               FROM P
               WHERE Color='Red'))))
```

*Codes of the suppliers
of the products
supplied by suppliers
of red products*

Complete query (no.3)

```
SELECT SName
FROM S
WHERE SId IN
    (SELECT SId
     FROM SP
     WHERE PId IN
         (SELECT PId
          FROM SP
          WHERE SId IN
              (SELECT SId
               FROM SP
               WHERE PId IN
                   (SELECT PId
                    FROM P
                    WHERE Color='Red'))));
```

Formulation with join (no.3)



Formulation with join (no.3)

```
SELECT SName
FROM S
WHERE SId IN
    (SELECT SId
     FROM SP
     WHERE PId IN
         (SELECT PId
          FROM SP
          WHERE SId IN
              (SELECT SId
               FROM SP
               WHERE PId IN
                   (SELECT PId
                    FROM P
                    WHERE Color='Red'))));
```

FROM clause (no.3)

```
SELECT SName
FROM (S)
WHERE SId IN
    (SELECT SId
     FROM (SP)
     WHERE PId IN
         (SELECT PId
          FROM (SP)
          WHERE SId IN
              (SELECT SId
               FROM (SP)
               WHERE PId IN
                   (SELECT PId
                    FROM (P)
                    WHERE Color='Red'))));
```

FROM clause (no.3)

```
SELECT SName
FROM (S)
WHERE SId IN
  (SELECT SId
   FROM (SP)
   WHERE PId IN
     (SELECT PId
      FROM (SP)
      WHERE SId IN
        (SELECT SId
         FROM (SP)
         WHERE PId IN
           (SELECT PId
            FROM (P)
            WHERE Color='Red')))))));
```

SPA

SPB

SPC

The diagram illustrates a nested SQL query structure. The main query is a SELECT statement with a FROM clause containing a subquery (S). This subquery (S) has a WHERE clause with an IN operator that points to another subquery (SP). This subquery (SP) has a WHERE clause with an IN operator that points to a third subquery (SP). This subquery (SP) has a WHERE clause with an IN operator that points to a fourth subquery (SP). This subquery (SP) has a WHERE clause with an IN operator that points to a fifth subquery (P). The annotations SPA, SPB, and SPC are red text labels with arrows pointing to the FROM clause of the first, second, and third subqueries respectively.

FROM clause (no.3)

SELECT ...

FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P

...

Join conditions (no.3)

```
SELECT SName      1
FROM S
WHERE SId IN
  (SELECT SId
   FROM SP
   WHERE PId IN
     (SELECT PId
      FROM SP
      WHERE SId IN
        (SELECT SId
         FROM SP
         WHERE PId IN
           (SELECT PId
            FROM P
            WHERE Color='Red'))));
```

The diagram illustrates the join conditions in the provided SQL query. A blue circle highlights the 'SId' attribute in the 'WHERE' clause of the outer query. A blue arc labeled '1' connects this 'SId' to the 'SId' attribute in the subquery '(SELECT SId FROM SP)'. A red circle highlights the 'SP' table name in the subquery, with a red arrow labeled 'SPA' pointing to it.

Join conditions (no.3)

SELECT ...

FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P

WHERE S.SId=SPA.SId

1

...

Join conditions (no.3)

```
SELECT SName  
FROM S  
WHERE SId IN
```

```
(SELECT SId  
FROM SP  
WHERE PId IN  
(SELECT PId  
FROM SP  
WHERE SId IN  
(SELECT SId  
FROM SP  
WHERE PId IN  
(SELECT PId  
FROM P  
WHERE Color='Red'))));
```

SPA

2

SPB

Join conditions (no.3)

```
SELECT ...  
FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P  
WHERE S.SId=SPA.SId AND  
      SPA.PId=SPB.PId  
      ...
```

2

Join conditions (no.3)

```
SELECT SName  
FROM S  
WHERE SId IN
```

```
(SELECT SId  
FROM SP
```

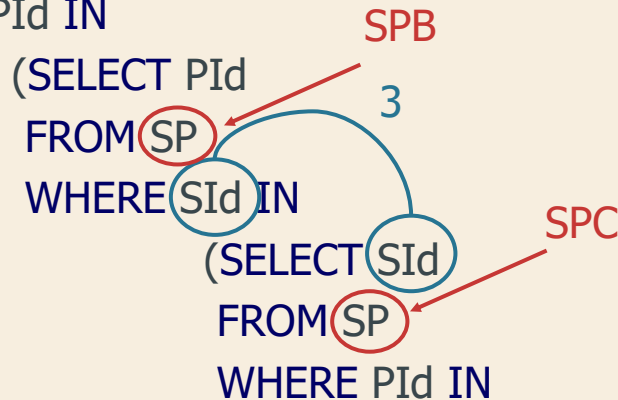
```
WHERE PId IN
```

```
(SELECT PId  
FROM SP  
WHERE SId IN
```

```
(SELECT SId  
FROM SP  
WHERE PId IN
```

```
(SELECT PId  
FROM P
```

```
WHERE Color='Red'))))));
```



Join conditions (no.3)

```
SELECT ...  
FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P  
WHERE S.SId=SPA.SId AND  
      SPA.PId=SPB.PId AND  
      SPB.SId=SPC.SId  
...
```

3

Join conditions (no.3)

```
SELECT SName
FROM S
WHERE SId IN
    (SELECT SId
     FROM SP
     WHERE PId IN
         (SELECT PId
          FROM SP
          WHERE SId IN
              (SELECT SId
               FROM SP
               WHERE PId IN
                   (SELECT PId
                    FROM P
                    WHERE Color='Red')))))));
```

The diagram highlights the join conditions in the provided SQL query. It shows a series of nested subqueries. The innermost subquery is `(SELECT PId FROM P WHERE Color='Red')`. This is joined to `SP` in the next level: `(SELECT PId FROM SP WHERE SId IN (SELECT SId FROM SP WHERE PId IN (SELECT PId FROM P WHERE Color='Red'))))`. This is then joined to `SP` in the next level: `(SELECT SId FROM SP WHERE PId IN (SELECT PId FROM SP WHERE SId IN (SELECT SId FROM SP WHERE PId IN (SELECT PId FROM P WHERE Color='Red'))))`. Finally, this is joined to `S` in the outermost query: `(SELECT SId FROM S WHERE SId IN (SELECT SId FROM SP WHERE PId IN (SELECT PId FROM SP WHERE SId IN (SELECT SId FROM SP WHERE PId IN (SELECT PId FROM P WHERE Color='Red'))))))`. The annotations include: a red arrow labeled 'SPC' pointing to the 'SP' table in the innermost subquery; a blue circle around 'SP' in the innermost subquery; a blue circle around 'PId' in the innermost subquery; a blue circle around 'PId' in the middle subquery; and a blue arc connecting the 'SP' in the middle subquery to the 'PId' in the innermost subquery with the number '4' below it.

Join conditions (no.3)

```
SELECT ...  
FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P  
WHERE S.SId=SPA.SId AND  
      SPA.PId=SPB.PId AND  
      SPB.SId=SPC.SId AND  
      SPC.PId=P.PId  
...
```

4

Selection predicate (no.3)

```
SELECT SName
FROM S
WHERE SId IN
    (SELECT SId
     FROM SP
     WHERE PId IN
         (SELECT PId
          FROM SP
          WHERE SId IN
              (SELECT SId
               FROM SP
               WHERE PId IN
                   (SELECT PId
                    FROM P
                    WHERE Color='Red'))));
```

Selection predicate (no.3)

```
SELECT ...  
FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P  
WHERE S.SId=SPA.SId AND  
       SPA.PId=SPB.PId AND  
       SPB.SId=SPC.SId AND  
       SPC.PId=P.PId AND  
       Color='Red'
```

SELECT statement (no.3)

```
SELECT DISTINCT SName
FROM S, SP AS SPA, SP AS SPB, SP AS SPC, P
WHERE S.SId=SPA.SId AND
      SPA.PId=SPB.PId AND
      SPB.SId=SPC.SId AND
      SPC.PId=P.PId AND
      Color='Red';
```



Nested queries

The NOT IN operator

Concept of exclusion (no.1)

- Find the names of the suppliers that *do not* supply product P2
- is it possible to express the query with a join operation?

```
SELECT SName
FROM S, SP
WHERE S.SId=SP.SId
      AND PId<>'P2';
```

Wrong solution (no.1)

- Find the names of the suppliers that *do not* supply product P2
- the query may not be expressed by means of a join

```
SELECT SName  
FROM S, SP  
WHERE S.SId=SP.SId  
AND PId<>'P2';
```


Wrong solution (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

R



SName
Smith
Jones
Clark

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

Wrong solution (no.1)

```
SELECT SName  
FROM S, SP  
WHERE S.SId=SP.SId  
      AND PId<>'P2';
```

➤ Which query does it answer?

Wrong solution (no.1)

```
SELECT SName  
FROM S, SP  
WHERE S.SId=SP.SId  
      AND PId<>'P2';
```



Find the names of the suppliers that supply
at least one product other than P2

Concept of exclusion (no.1)

- Find the names of the suppliers that *do not* supply product P2
- We need to exclude from the result
 - the suppliers that supply product P2

Concept of exclusion (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

```
SELECT SId  
FROM SP  
WHERE PId='P2'
```


*Codes of the suppliers
that supply P2*

Concept of exclusion (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

```
SELECT SName  
FROM S  
WHERE SId
```

```
(SELECT SId  
FROM SP  
WHERE PId='P2');
```



*Codes of the suppliers
that supply P2*

The NOT IN operator (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

```
SELECT SName
FROM S
WHERE SId NOT IN (SELECT SId
                  FROM SP
                  WHERE PId='P2');
```

does not belong to

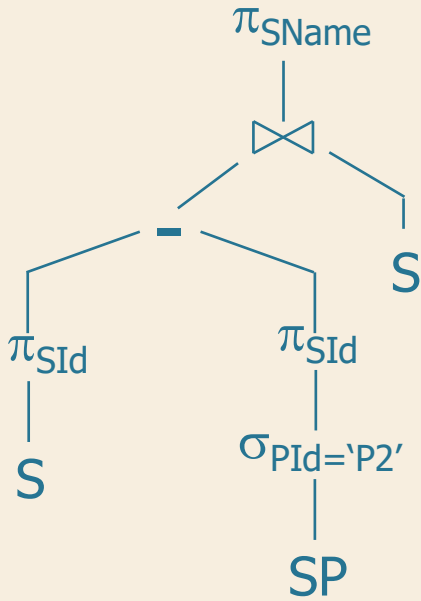
*Codes of the suppliers
that supply P2*

The NOT IN operator

- It expresses the concept of exclusion from a set of values
 - *AttributeName* NOT IN (*NestedQuery*)
- It requires the identification of an appropriate *set to be excluded*
 - defined by the nested query

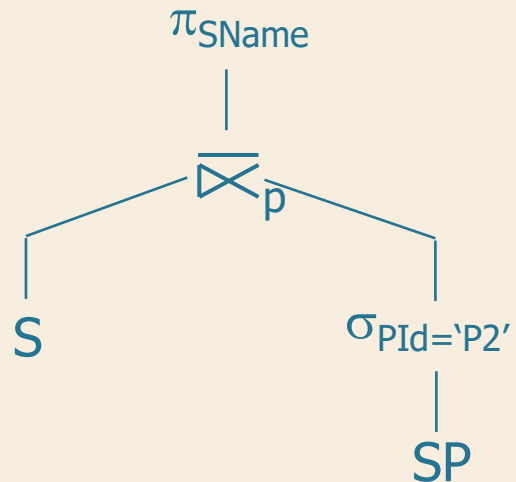
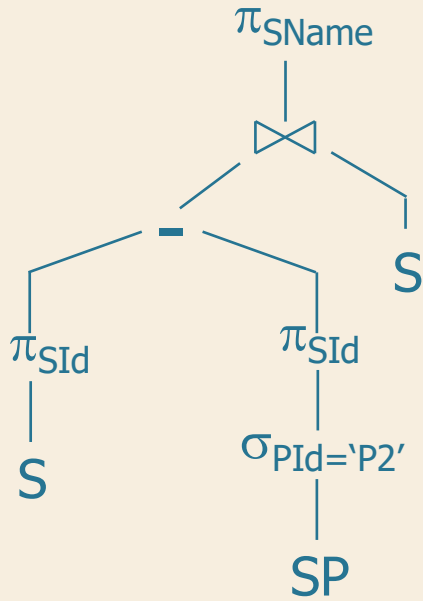
NOT IN and relational algebra (no.1)

➤ Find the names of the suppliers that *do not* supply product P2



NOT IN and relational algebra (no.1)

➤ Find the names of the suppliers that *do not* supply product P2



p: S.SId=SP.SId

The NOT IN operator (no.2)

- Find the names of the suppliers that *only* supply product P2



Find the names of the suppliers of P2 that have never supplied products other than P2

- Set to be excluded
 - suppliers of products other than P2

The NOT IN operator (no.2)

➤ Find the names of the suppliers that only supply product P2

```
SELECT SId  
FROM SP  
WHERE PId <> 'P2'
```

*Codes of the suppliers
that supply
at least one product
other than P2*

The NOT IN operator (no.2)

- Find the names of the suppliers that only supply product P2

```
SELECT SName
FROM S
WHERE SId NOT IN (SELECT SId
                  FROM SP
                  WHERE PId<>'P2')
```

...

The NOT IN operator (no.2)

- Find the names of the suppliers that only supply product P2

```
SELECT SName
FROM S, SP
WHERE S.SId NOT IN (SELECT SId
                    FROM SP
                    WHERE PId<>'P2')
AND S.SId=SP.SId;
```


Alternative solution (no.2)

- Find the names of the suppliers that only supply product P2

```
SELECT SName
FROM S
WHERE S.SId NOT IN (SELECT SId
                    FROM SP
                    WHERE PId<>'P2')
AND S.SId IN (SELECT SId
              FROM SP);
```

The NOT IN operator (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

➤ P (PId, PName, Color, Size, Store)

➤ S (SId, SName, #Employees, City)

➤ SP (SId, PId, Qty)

The NOT IN operator (no.3)

- Find the names of the suppliers that *do not* supply any red products
- Set to be excluded?
 - suppliers of red products, identified by their codes

The NOT IN operator (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

*Codes of the suppliers
of red products*

```
(SELECT SId
FROM SP
WHERE PId IN (SELECT PId
FROM P
WHERE Color='Red'))
```

The NOT IN operator (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

```
SELECT SName
FROM S
WHERE SId NOT IN (SELECT SId
                  FROM SP
                  WHERE PId IN (SELECT PId
                               FROM P
                               WHERE Color='Red'));
```

Alternative (correct?) (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

Codes of the suppliers that supply at least one non-red product

```
SELECT SId
FROM SP
WHERE PId NOT IN (SELECT PId
                  FROM P
                  WHERE Color='Red')
```

Alternative (correct?) (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId NOT IN (SELECT PId
                                FROM P
                                WHERE Color='Red'));
```

Wrong alternative (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

```
SELECT SName  
FROM S  
WHERE SId IN (SELECT SId  
              FROM SP  
              WHERE PId NOT IN (SELECT PId  
                                FROM P  
                                WHERE Color='Red')));
```


Wrong alternative (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

```
SELECT SName
FROM S
WHERE SId IN (SELECT SId
              FROM SP
              WHERE PId NOT IN (SELECT PId
                                FROM P
                                WHERE Color='Red'));
```

Codes of the suppliers of non-red products

Wrong alternative (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

P

<u>PId</u>	<u>PName</u>	<u>Color</u>	<u>Size</u>	<u>Store</u>
P1	Jumper	Red	40	London
P2	Jeans	Green	48	Paris
P3	Blouse	Blue	48	Rome
P4	Blouse	Red	44	London
P5	Skirt	Blue	40	Paris
P6	Shorts	Red	42	London

S

<u>SId</u>	<u>SName</u>	<u>#Employees</u>	<u>City</u>
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	<u>Qty</u>
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

Wrong alternative (no.3)

➤ Find the names of the suppliers that *do not* supply any red products

P

<u>PId</u>	<u>PName</u>	<u>Color</u>	<u>Size</u>	<u>Store</u>
P1	Jumper	Red	40	London
P2	Jeans	Green	48	Paris
P3	Blouse	Blue	48	Rome
P4	Blouse	Red	44	London
P5	Skirt	Blue	40	Paris
P6	Shorts	Red	42	London

S

<u>SId</u>	<u>SName</u>	<u>#Employees</u>	<u>City</u>
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	<u>Qty</u>
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

Wrong alternative (no.3)

- Find the names of the suppliers that *do not* supply any red products

```
SELECT SName  
FROM S  
WHERE SId IN (SELECT SId  
              FROM SP  
              WHERE PId NOT IN (SELECT PId  
                                FROM P  
                                WHERE Color='Red')));
```

- The set of elements to be excluded is incorrect



Nested queries

The tuple constructor

The tuple constructor

- It allows defining a temporary structure for a tuple
 - the attributes belonging to the tuple must be listed within ()

(AttributeName₁, AttributeName₂, ...)

- It enhances the expressive power of the **IN** and **NOT IN** operators

Example (no.1)

TRIP (TId, StartingPlace, Destination,
DepartureTime, ArrivalTime)

- Find the pairs of starting places and destinations for which none of the trips lasts more than 2 hours

Example (no.1)

TRIP (TId, StartingPlace, Destination,
DepartureTime, ArrivalTime)

- Find the pairs of starting places and destinations for which none of the trips lasts more than 2 hours

```
SELECT StartingPlace, Destination
FROM TRIP
WHERE (StartingPlace, Destination) NOT IN
      (SELECT StartingPlace, Destination
       FROM TRIP
       WHERE ArrivalTime-DepartureTime>2);
```

*Tuple
constructor*



Nested queries

The EXISTS operator

The EXISTS operator (no.1)

➤ Find the names of the suppliers of product P2



*Find the names of the suppliers for which
there exists a product supply for P2*

Correlation condition (no.1)

➤ Find the names of the suppliers of product P2

```
SELECT SName
FROM S
WHERE EXISTS (SELECT *
              FROM SP
              WHERE PId='P2'
              AND SP.SId=S.SId );
```

Correlation condition

How EXISTS works (no.1)

➤ Find the names of the suppliers of product P2

S

SId	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

SId	PId	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

```
SELECT *  
FROM SP  
WHERE PId='P2'
```

```
AND SP.SId='S1'
```

↑
*Value of SId in the
current line of table S*

How EXISTS works (no.1)

➤ Find the names of the suppliers of product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

➤ The predicate including **EXISTS** is true for S1 since there exists a supply for P2 by S1

- S1 belongs to the result of the query

How EXISTS works (no.1)

➤ Find the names of the suppliers of product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

➤ The predicate including **EXISTS** is false for S4 since there exists no supply for P2 by S4

- S4 is not included in the result of the query

Result of the query (no.1)

➤ Find the names of the suppliers of product P2

R

SName
Smith
Jones
Blake

Predicates with EXISTS

- The predicate including EXISTS is
- true if the inner query returns at least one tuple
 - false if the inner query returns the empty set

Predicates with EXISTS

- The predicate including **EXISTS** is
 - true if the inner query returns at least one tuple
 - false if the inner query returns the empty set
- In the query inside **EXISTS**, the **SELECT** clause is mandatory but irrelevant, since its attributes are never displayed
- The correlation condition binds the execution of the inner query to the values of attributes of the current tuple in the outer query

Scope of attributes

- A nested query may reference attributes defined within outer queries
- A query may not reference attributes defined
 - within a nested query at an inner level
 - within a different query at the same level



Nested queries

The NOT EXISTS operator

The NOT EXISTS operator (no.1)

➤ Find the names of the suppliers that *do not* supply product P2



Find the names of the suppliers for which there does not exist a product supply for P2

The NOT EXISTS operator (no.1)

➤ Find the names of the suppliers that *do not* supply product P2


```
SELECT SName
FROM S
WHERE NOT EXISTS (SELECT *
                  FROM SP
                  WHERE PId='P2'
                  AND SP.SId=S.SId );
```

Correlation condition

How NOT EXISTS works (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S



<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

```
SELECT *
```

```
FROM SP
```

```
WHERE PId='P2' AND
```

```
SP.SId='S1'
```

*value of SId in the
current line of table S*

How NOT EXISTS works (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S



<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP




<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

```
SELECT *  
FROM SP  
WHERE PId='P2' AND  
       SP.SId='S1'
```


How NOT EXISTS works (no.1)


➤ Find the names of the suppliers that *do not* supply product P2

S



<u>SId</u>	<u>SName</u>	<u>#Employees</u>	<u>City</u>
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP



<u>SId</u>	<u>PId</u>	<u>Qty</u>
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400


➤ The predicate including **NOT EXISTS** is false for S1 since there exists a supply for P2 by F1

- S1 *does not* belong to the result of the query

How NOT EXISTS works (no.1)


➤ Find the names of the suppliers that *do not* supply product P2

S



<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP



<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

How NOT EXISTS works (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens



How NOT EXISTS works (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

How NOT EXISTS works (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

➤ The predicate including **NOT EXISTS** is true of S4 since there exists no supply for P2 by S4

- S4 belongs to the result of the query

How NOT EXISTS works (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

S

<u>SId</u>	SName	#Employees	City
S1	Smith	20	London
S2	Jones	10	Paris
S3	Blake	30	Paris
S4	Clark	20	London
S5	Adams	30	Athens

SP

<u>SId</u>	<u>PId</u>	Qty
S1	P1	300
S1	P2	200
S1	P3	400
S1	P4	200
S1	P5	100
S1	P6	100
S2	P1	300
S2	P2	400
S3	P2	200
S4	P3	200
S4	P4	300
S4	P5	400

Result of the query (no.1)

➤ Find the names of the suppliers that *do not* supply product P2

R

SName
Clark
Adams

Predicates with NOT EXISTS

- The predicate including NOT EXISTS is
 - true if the inner query returns the empty set
 - false if the inner query return at least one tuple
- The correlation condition binds the execution of the inner query to the values of attributes of the current tuple in the outer query



Nested queries

Correlation among queries

Correlation among queries

- It may be required to bind the computation of a nested query to the value(s) of one or more attributes in an outer query
 - the binding is expressed by one or more correlation conditions

Correlation condition

➤ A correlation condition

- must be specified in the WHERE clause of the nested query that requires it
- is a predicate that binds some attributes of tables appearing in the nested query's FROM clause to attributes of tables appearing in the FROM clause of outer queries

➤ Correlation conditions may not be expressed

- within queries at the same nesting level
- with references to attributes of a table appearing in the FROM clause of a nested query

Correlation among queries (no.1)

- For each product, find the code of the supplier that provides the highest quantity

Correlation among queries (no.1)

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT PId, SId  
FROM SP AS SPX  
WHERE Qty = (...
```

```
)
```

*Maximum
quantity
for the current
product*

Correlation among queries (no.1)

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT PId, SId  
FROM SP AS SPX  
WHERE Qty = (SELECT MAX(Qty)  
             FROM SP AS SPY  
             ... )
```

*Maximum
quantity*

Correlation among queries (no.1)

➤ For each product, find the code of the supplier that provides the highest quantity

```
SELECT PId, SId
FROM SP AS SPX
WHERE Qty = (SELECT MAX(Qty)
             FROM SP AS SPY
             WHERE SPY.PId=SPX.PId);
```

*Maximum
quantity
for the current
product*

Correlation among queries (no.1)

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT PId, SId
FROM SP AS SPX
WHERE Qty = (SELECT MAX(Qty)
             FROM SP AS SPY
             WHERE SPY.PId=SPX.PId);
```

Correlation condition

Correlation among queries (no.1) – Alternative solution

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT Sid
FROM SP AS SPX
WHERE (PID, QTY) IN (SELECT PID, Max(Qty)
                    FROM SP
                    GROUP BY PID)
```


Correlation among queries (no.1) – Wrong solution

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT Sid  
FROM SP AS SPX  
WHERE QTY = (SELECT Max(Qty)  
FROM SP  
GROUP BY PID)
```

Correlation among queries (no.1) – Wrong solution

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT Sid  
FROM SP AS SPX  
WHERE QTY = (SELECT Max(Qty)  
FROM SP)
```

Correlation among queries (no.1) – Wrong solution

- For each product, find the code of the supplier that provides the highest quantity

```
SELECT Sid  
FROM SP AS SPX  
WHERE QTY = (SELECT Max(Qty)  
FROM SP SPY  
WHERE SPY.PID=SPX.PID  
GROUP BY PID)
```

Correlation among queries (no.2)

TRIP (TId, StartingPlace, Destination,
DepartureTime, ArrivalTime)

- Find the codes of the trips whose duration is lower than the average duration of the trips on the same route (i.e., same starting place and destination)

```
SELECT TId  
FROM TRIP AS TA  
WHERE ArrivalTime-DepartureTime < (...
```

} *Average
duration
of trips
on the current
route*

Correlation among queries (no.2)

TRIP (TId, StartingPlace, Destination,
DepartureTime, ArrivalTime)

- Find the codes of the trips whose duration is lower than the average duration of the trips on the same route (i.e., same starting place and destination)

```
SELECT TId
FROM TRIP AS TA
WHERE ArrivalTime-DepartureTime <
      (SELECT AVG(ArrivalTime-DepartureTime)
       FROM TRIP AS TB
       ... )
```

*Average
duration
of trips*

Correlation among queries (no.2)

TRIP (TId, StartingPlace, Destination,
DepartureTime, ArrivalTime)

- Find the codes of the trips whose duration is lower than the average duration of the trips on the same route (i.e., same starting place and destination)

```
SELECT TId
FROM TRIP AS TA
WHERE ArrivalTime-DepartureTime <
      (SELECT AVG(ArrivalTime-DepartureTime)
       FROM TRIP AS TB
        WHERE TB.StartingPlace=TA.StartingPlace
              AND TB.Destination=TA.Destination);
```

Correlation conditions



Nested queries

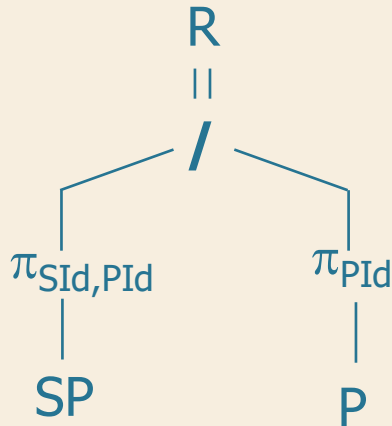
The division operation

The division operation (no.1)

- Find the codes of the suppliers that supply *all* products
- In relational algebra we must use the division operator

The division operation (no.1)

- Find the codes of the suppliers that supply *all* products
- In relational algebra we must use the division operator



Division in SQL (no.1)

➤ Find the codes of the suppliers that supply *all* products

➤ Remark

- all products that may be supplied are listed in table P



- a supplier is supplying all products if he is supplying a number of distinct products equal to the cardinality of P

Division in SQL (no.1)

➤ Find the codes of the suppliers that supply *all* products

```
SELECT COUNT(*)  
FROM P
```

Division in SQL (no.1)

➤ Find the codes of the suppliers that supply *all* products

```
SELECT COUNT(*)  
FROM P
```

} *Total
number
of products*

Division in SQL (no.1)

➤ Find the codes of the suppliers that supply *all* products

```
SELECT SId  
FROM SP  
GROUP BY SId
```

...

```
(SELECT COUNT(*)  
FROM P)
```

Division in SQL (no.1)

➤ Find the codes of the suppliers that supply *all* products

SP(SID, PID, Qty)

```
SELECT SId
FROM SP
GROUP BY SId
HAVING COUNT(*)=(SELECT COUNT(*)
                   FROM P);
```

Division in SQL (no.1) – Different SP TABLE

➤ Find the codes of the suppliers that supply *all* products

SP(SID, PID, Date, Qty)

SELECT SId

FROM SP

GROUP BY SId

HAVING COUNT(**DISTINCT PID**)=(SELECT COUNT(*)
FROM P);

Division in SQL: procedure (no.2)

- Find the codes of the suppliers that supply at least *all* of the products supplied by supplier S2
- We must count
 - the number of products supplied by S2
 - the number of products supplied both by an arbitrary supplier and by S2
 - (Alternative formulation)
 - Among the products supplied by S2, count the number of products supplied by an arbitrary supplier

➤ The two counts must be equal

Division in SQL (no.2)

- Find the codes of the suppliers that supply at least *all* of the products supplied by supplier S2

```
SELECT COUNT(*)  
FROM SP  
WHERE SId='S2'
```

Division in SQL (no.2)

- Find the codes of the suppliers that supply at least *all* of the products supplied by supplier S2

```
SELECT COUNT(*)  
FROM SP  
WHERE SId='S2'
```

*Number of
products
supplied by S2*

Division in SQL (no.2)

➤ Find the codes of the suppliers that supply at least *all* of the products supplied by supplier S2

```
SELECT SId
FROM SP
WHERE PId IN (SELECT PId
              FROM SP
              WHERE SId='S2')
GROUP BY SId
... (SELECT COUNT(*)
      FROM SP
      WHERE SId='S2')
```

Division in SQL (no.2)

➤ Find the codes of the suppliers that supply at least *all* of the products supplied by supplier S2

```
SELECT SId
FROM SP
WHERE PId IN (SELECT PId
              FROM SP
              WHERE SId='S2')
GROUP BY SId
HAVING COUNT(*)=(SELECT COUNT(*)
                  FROM SP
                  WHERE SId='S2');
```



Nested queries

Table functions

Example schema

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

COURSE (CId, CName)

Computing two-level aggregates (no.1)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ Find the highest average (achieved by a student)

➤ 2-step solution

- find the average for each student
- find the maximum average value

Computing two-level aggregates (no.1)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ Find the highest average (achieved by a student)

- step 1: average for each student

```
SELECT SId, AVG(Grade) AS StudentAVG
FROM PASSED-EXAM
GROUP BY SId
```


Computing two-level aggregates (no.1)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ Find the highest average (achieved by a student)

- step 1: average for each student

```
(SELECT SId, AVG(Grade) AS StudentAVG  
FROM PASSED-EXAM  
GROUP BY SId) AS AVERAGES
```

Computing two-level aggregates (no.1)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ Find the highest average (achieved by a student)

- step 2: maximum average value

SELECT ...

FROM (SELECT SId, AVG(Grade) AS StudentAVG

FROM PASSED-EXAM

GROUP BY SId) AS AVERAGES

Computing two-level aggregates (no.1)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ Find the highest average (achieved by a student)

- step 2: maximum average value

```
SELECT MAX(StudentAVG)
```

```
FROM (SELECT SId, AVG(Grade) AS StudentAVG
```

```
FROM PASSED-EXAM
```

```
GROUP BY SId) AS AVERAGES;
```

Table functions (no.1)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ Find the highest average (achieved by a student)

```
SELECT MAX(StudentAVG)
```

```
FROM (SELECT SId, AVG(Grade) AS StudentAVG  
      FROM PASSED-EXAM  
      GROUP BY SId) AS AVERAGES;
```

Table function

Table function

- It defines a temporary table that may be used for further computations
- The table function
 - has the structure of a `SELECT` statement
 - is defined within a `FROM` clause
 - may be referenced as a normal table
- Table functions allow
 - the computation of multi-level aggregates
 - an equivalent formulation of queries that require the use of correlation

Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

- For each year of enrolment, find the highest average (achieved by a student)

Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ For each year of enrolment, find the highest average (achieved by a student)

➤ 2-step solution

- find the average for each student
- group students by year of enrolment and compute the maximum average

Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ For each year of enrolment, find the highest average (achieved by a student)

- step 1

```
(SELECT SId, AVG(Grade) AS StudentAVG  
FROM PASSED-EXAM  
GROUP BY SId) AS AVERAGES
```


Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ For each year of enrolment, find the highest average (achieved by a student)

- step 2

SELECT ...

FROM STUDENT,

(SELECT SIId, AVG(Grade) AS StudentAVG

FROM PASSED-EXAM

GROUP BY SIId) AS AVERAGES

WHERE STUDENT.SIId=AVERAGES.SIId

Table function

...

Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ For each year of enrolment, find the highest average (achieved by a student)

● step 2

SELECT ...

FROM STUDENT,

(SELECT SIid, AVG(Grade) AS StudentAVG

FROM PASSED-EXAM

GROUP BY SIid) AS AVERAGES

WHERE STUDENT.SIid=AVERAGES.SIid

*Join
condition*

Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ For each year of enrolment, find the highest average (achieved by a student)

- step 2

```
SELECT ...
```

```
FROM STUDENT,
```

```
    (SELECT SId, AVG(Grade) AS StudentAVG
```

```
    FROM PASSED-EXAM
```

```
    GROUP BY SId) AS AVERAGES
```

```
WHERE STUDENT.SId=AVERAGES.SId
```

```
GROUP BY YearOfEnrolment
```

Table functions (no.2)

STUDENT (SId, YearOfEnrolment)

PASSED-EXAM (SId, CId, Date, Grade)

➤ For each year of enrolment, find the highest average (achieved by a student)

- step 2

```
SELECT YearOfEnrolment, MAX(StudentAVG)
```

```
FROM STUDENT,
```

```
    (SELECT SId, AVG(Grade) AS StudentAVG
```

```
    FROM PASSED-EXAM
```

```
    GROUP BY SId) AS AVERAGES
```

```
WHERE STUDENT.SId=AVERAGES.SId
```

```
GROUP BY YearOfEnrolment;
```