



Politecnico
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Data Science Lab

Scikit-learn
Regression

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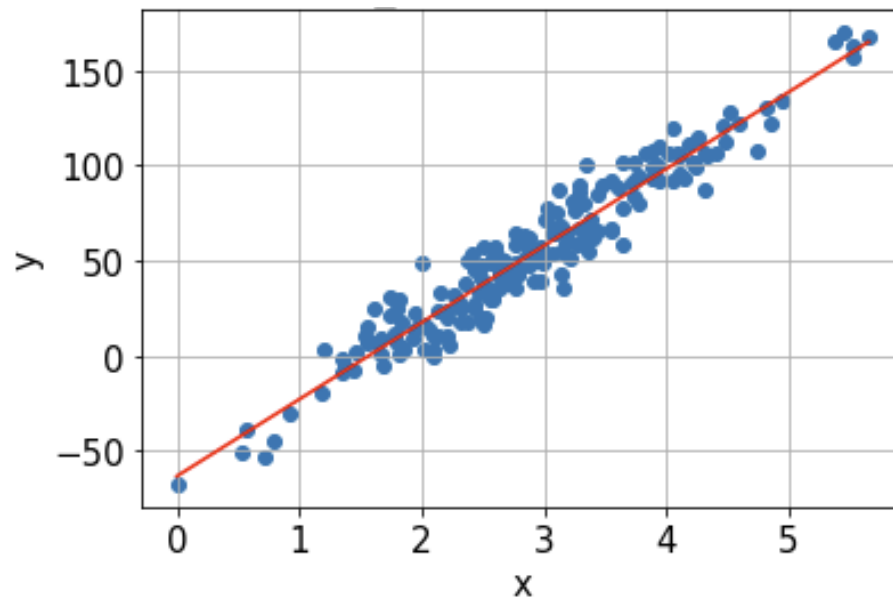
DataBase and Data Mining Group



Linear regression

- Regression with Scikit-learn

```
from sklearn.linear_model import LinearRegression  
reg = LinearRegression()  
reg.fit(X_train, y_train)  
y_test_pred = reg.predict(X_test)
```





- Evaluation metrics for regression:
 - MAE (Mean Absolute Error)
 - MSE (Mean Squared Error)
 - R^2

```
from sklearn.metrics import r2_score
from sklearn.metrics import mean_absolute_error
from sklearn.metrics import mean_squared_error

# Compute R2, MAE and MSE:
r2 = r2_score(y_test, y_test_pred)
mae = mean_absolute_error(y_test, y_test_pred)
mse = mean_squared_error(y_test, y_test_pred)
```



- Evaluation with `cross_val_score()`

```
from sklearn.model_selection import cross_val_score

reg = LinearRegression()
r2 = cross_val_score(reg, X, y, cv=5, scoring='r2')
```

- Parameters:

- `cv` = number of partitions for cross-validation
- `scoring` = scoring function for the evaluation
 - E.g. 'r2', '**neg**_mean_squared_error'

- Similarly, we can use `cross_val_predict()`



Notebook Examples

- **4b-Scikitlearn-Linear-Regression.ipynb**
 - 1. Simple linear regression
 - 2. Linear regression with multiple input features





- Polynomial regression
 - Useful when the data does not follow a linear trend
- **It consists of:**
 - Computing new **features** that are power functions of the input features
 - Applying **linear** regression on the new features

input vector = $[x_1, x_2]$



degree(2) features = $[1, x_1, x_2, x_1^2, x_2^2, x_1x_2]$



$$f(x) = w_0 + w_1x_1 + w_2x_2 + w_3x_1^2 + w_4x_2^2 + w_5x_1x_2$$



- Extracting polynomial features

```
from sklearn.preprocessing import PolynomialFeatures  
poly = PolynomialFeatures(5)  
X_poly = poly.fit_transform(X)
```

- Parameters:

- degree

- Integer: the maximal degree of the computed features
 - Tuple: min and max degrees of the computed features

- interaction_only: if True, only include interaction terms

- Exclude terms with power ≥ 2 of the same input feature

- include_bias: if True, add a bias column (column of ones)

- Output of fit_transform():

- A 2D **NumPy array** with the new feature matrix



- Building a **pipeline** with polynomial features and linear regression

```
from sklearn.pipeline import make_pipeline
reg = make_pipeline(PolynomialFeatures(5), LinearRegression())
reg.fit(X_train, y_train)
y_test_pred = reg.predict(X_test)
```

- Pipelines are objects that allow concatenating multiple Scikit-learn models
 - N-1 transformers, 1 final predictor



■ Ridge:

```
from sklearn.linear_model import Ridge  
reg = Ridge(alpha=0.5)
```

■ Lasso:

```
from sklearn.linear_model import Lasso  
reg = Lasso(alpha=0.5)
```



Notebook Examples

- **4c-Scikitlearn-Polynomial-Regression.ipynb**
 - 1. Polynomial regression
 - 2. Overfitting and regularization





- Hyperparameters vs parameters
 - Hyperparameters are selected by the user
 - Parameters are computed by the algorithm during training
- **Important:** hyperparameters cannot be set by finding the values that give the best results on the test set
 - This methodology **will overfit the test set**
 - We would be using **information from the test data** to select some **training** hyperparameters



- Step 1. define the grid of all hyperparameters
 - A **dictionary** with the **parameter values** that to tune
 - E.g. for Ridge regression:

```
param_grid = {'alpha' : [0.1, 0.2],  
              'fit_intercept' : [True, False]}
```

- ParameterGrid() enumerates all possible combinations
- Scikit-learn will try all the **combinations**:
 - {alpha=0.1,fit_intercept=True}
 - {alpha=0.1,fit_intercept=False}
 - {alpha=0.2,fit_intercept=True}
 - {alpha=0.2,fit_intercept=False}



- Step 2. Define a model, and call GridSearchCV

```
from sklearn.model_selection import GridSearchCV
reg = Ridge()
gridsearch = GridSearchCV(reg, param_grid, scoring='r2', cv=5)
gridsearch.fit(X_train, y_train)
```

- This code will pick the best configuration of the param grid, for Ridge model,
 - According to the R^2 score
 - Using a cross validation with **k=5** partitions
- Passing `n_jobs=-1`, parallelizes across all available processors



- The best parameter configuration can be found in the *best_params_* attribute of the gridsearch object
- An instance of the model with the best configuration is available in *best_estimator_*
 - **Important:** it is trained on the **whole dataset!**

```
...  
gridsearch.fit(X_train, y_train)  
print(gridsearch.best_params_['alpha'])  
print(gridsearch.best_params_['fit_intercept'])  
  
best_configured_model = gridsearch.best_estimator_
```



- RandomizedSearchCV()
 - Same params as GridSearchCV()
 - An additional `n_iter=[number]` defines the total number of configurations to try
- BayesSearchCV()
 - Not in scikit-learn, but in scikit-optimize
 - <https://scikit-optimize.github.io/>
 - Uses Bayesian optimization
 - Same params as RandomizedSearchCV()
 - The optimizer can be configured via `optimizer_kwargs`



Notebook Examples

- **4c-Scikitlearn-Polynomial-Regression.ipynb**
 - **3. Grid-search to select model hyperparameters**

