

Visual Perception

Data Management and Visualization



SoftEng
<http://softeng.polito.it>

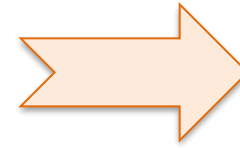
Version 1.7.1
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VISUALIZATION PIPELINE

Visualization Pipeline

Knowledge



Decisions

Information Understanding

Visual Patterns, Trends, Exceptions

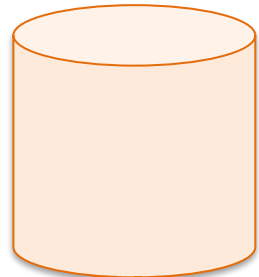
Quantitative Reasoning

Quantitative Relationship & Comparison

Visual Perception

Visual Properties & Objects

Data

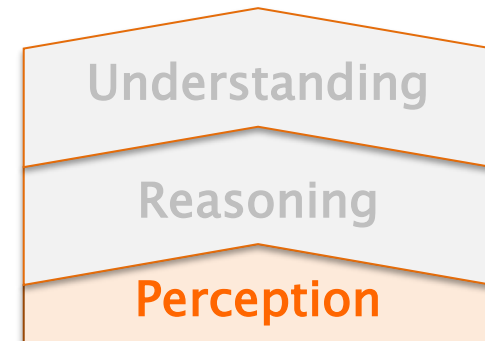


Representation/Encoding



Visual Perception

- Any variable (measure) must be **visually encoded**, i.e. we need to identify:
 - ◆ Visual object to represent entity
 - ◆ Visual attribute to represent the measure



Example

Votes received by four candidates in recent elections

Candidate	Votes	Proportion
Sergio	1 97800	50.09%
Alberto	1 40545	35.59%
Giorgio	53748	13.61%
Valter	2759	0.70%

Encoding

- Visual object: line
- Visual attribute: length

Alberto

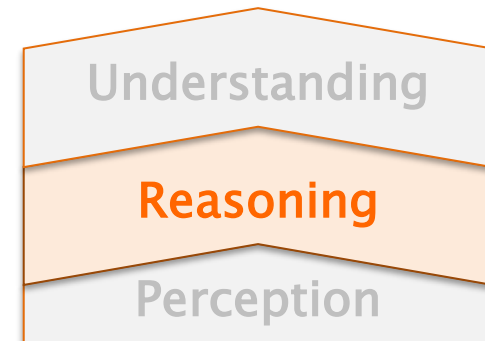
- Giorgio
Valter

Sergio

Visual Reasoning

Layout and visual attributes allow:

- **Discrimination**
 - ◆ Distinguish visual objects or group of –
- **Comparison**
 - ◆ Place visual objects in order
- **Magnitude assessment**
 - ◆ Evaluate the (relative) magnitude of visual objects



Reasoning

- Discrimination

Alberto

- Giorgio
Valter

Sergio

Reasoning

- Comparison



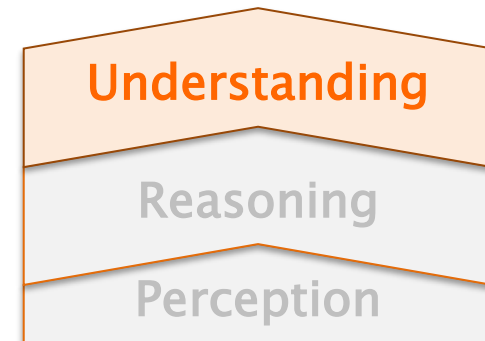
Reasoning

- Assessment



Understanding

- Variation within quantitative measures
 - ◆ Distribution
 - ◆ Deviation
 - ◆ Correlation
- Variation within category
 - ◆ Ranking
 - ◆ Part-to-whole
 - ◆ Time
 - ◆ Space
- Multivariate



Understanding

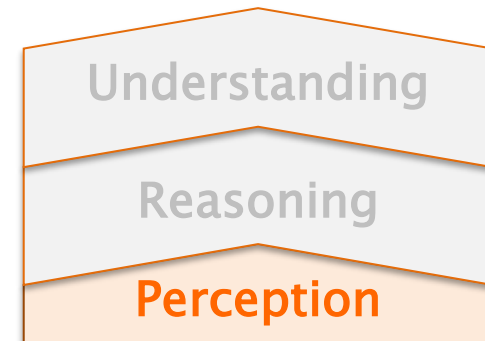


Understanding

- Ranking



VISUAL PERCEPTION



Visual perception

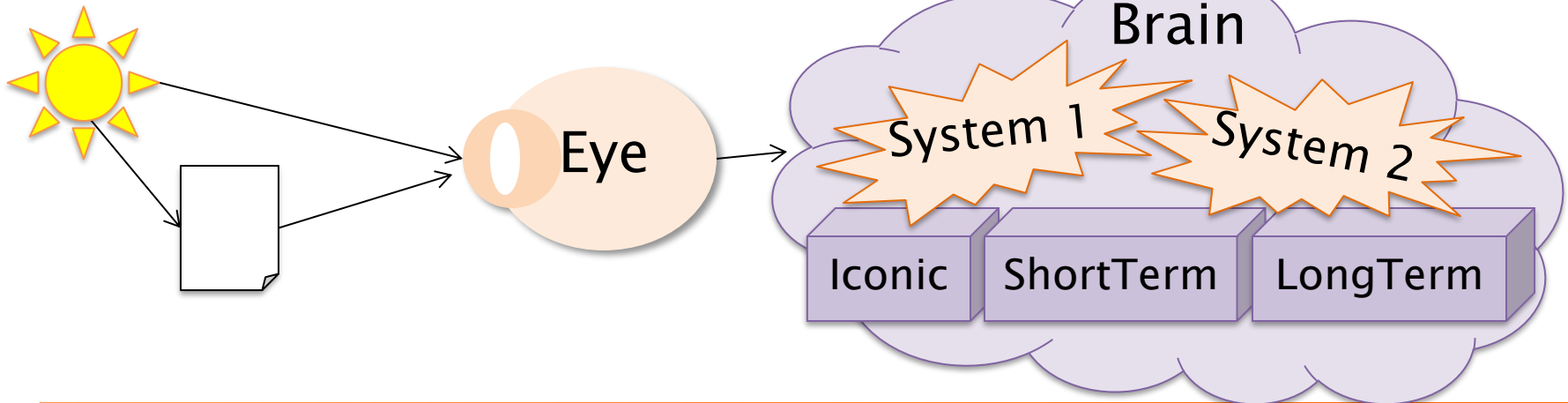
Sensation
(Physical process)

Perception
(Cognitive process)

Stimulus

Sensory Organ

Perceptual Organ



Memory Hierarchy

- Iconic memory (visual sensory register)
 - ◆ Pre-attentive processing
 - ◆ Detects a **limited number of attributes**
- Short-term memory (working memory)
 - ◆ Store visual chunks
 - ◆ Limited number
- Long-term memory
 - ◆ Store high-level knowledge

Simplified Model

- The three levels of memory represent a simplified model
 - ◆ does not correspond to “real” physical structure
- Useful to explain a few phenomena
 - ◆ The 7 ± 2 rule
 - ◆ Change blindness

Change blindness



Pre-Attentive Attributes

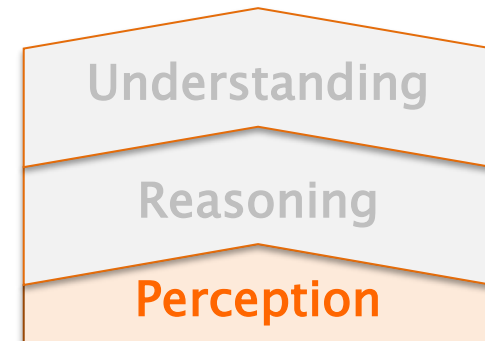
5	7	8	4	9	8	3	1	1	0	6	8	8	2	1	1	5	2	6	6	5
9	5	1	8	4	6	8	4	9	3	0	4	5	3	4	9	2	5	8	5	8
5	0	5	4	6	2	6	5	7	3	7	8	6	5	3	7	2	6	3	1	5
5	8	6	6	8	3	7	6	5	0	9	6	3	4	6	1	9	5	6	6	4
1	6	7	3	9	9	2	8	3	4	0	3	5	1	6	3	5	3	9	3	4
8	6	9	7	5	4	2	4	7	4	9	5	8	5	3	0	7	6	0	6	7
0	3	1	5	3	2	3	5	6	7	2	8	9	8	5	3	7	8	8	2	4
5	5	3	4	8	1	5	6	2	3	5	5	1	2	1	0	8	7	2	6	3
7	4	3	8	4	8	2	6	7	9	5	6	2	3	6	7	8	0	8	3	6
4	9	5	6	7	2	2	2	8	3	1	1	0	1	8	6	2	6	2	1	4

Pre-Attentive Attributes

5	7	8	4	9	8	3	1	1	0	6	8	8	2	1	1	5	2	6	6	5
9	5	1	8	4	6	8	4	9	3	0	4	5	3	4	9	2	5	8	5	8
5	0	5	4	6	2	6	5	7	3	7	8	6	5	3	7	2	6	3	1	5
5	8	6	6	8	3	7	6	5	0	9	6	3	4	6	1	9	5	6	6	4
1	6	7	3	9	9	2	8	3	4	0	3	5	1	6	3	5	3	9	3	4
8	6	9	7	5	4	2	4	7	4	9	5	8	5	3	0	7	6	0	6	7
0	3	1	5	3	2	3	5	6	7	2	8	9	8	5	3	7	8	8	2	4
5	5	3	4	8	1	5	6	2	3	5	5	1	2	1	0	8	7	2	6	3
7	4	3	8	4	8	2	6	7	9	5	6	2	3	6	7	8	0	8	3	6
4	9	5	6	7	2	2	2	8	3	1	1	0	1	8	6	2	6	2	1	4

Encoding

- Encoding is the key to enable visual perception
 - ◆ Visual object to represent entity
 - ◆ Visual attribute to represent the measure
- Two main types
 - ◆ Quantitative (different properties)
 - ◆ Categorical (ordinal or not)



Pre-Attentive attributes

Category	Attribute
Form	Orientation Length/distance Line width Size Shape Curvature Added marks Enclosure
Color	Hue Intensity
Spatial position	2-D position
Motion	Flicker Direction Speed

Perception task

Visual attributes allow:

- Discrimination
 - ◆ Distinguish visual objects
- Comparison
 - ◆ Place visual objects in order
- Magnitude assessment
 - ◆ Evaluate the (relative) magnitude of visual objects

Just noticeable difference

- Given a physical dimension (length, brightness, etc.) x
- d is the **just noticeable difference** if:
 - ◆ difference between x and $x+d$ is perceivable
 - ◆ but not smaller differences
- d depends on many factors:
 - ◆ Subject
 - ◆ Environment
 - ◆ Physical dimension

Weber's law

- Just noticeable difference d is:

$$d_p(x) = k_p \cdot x$$

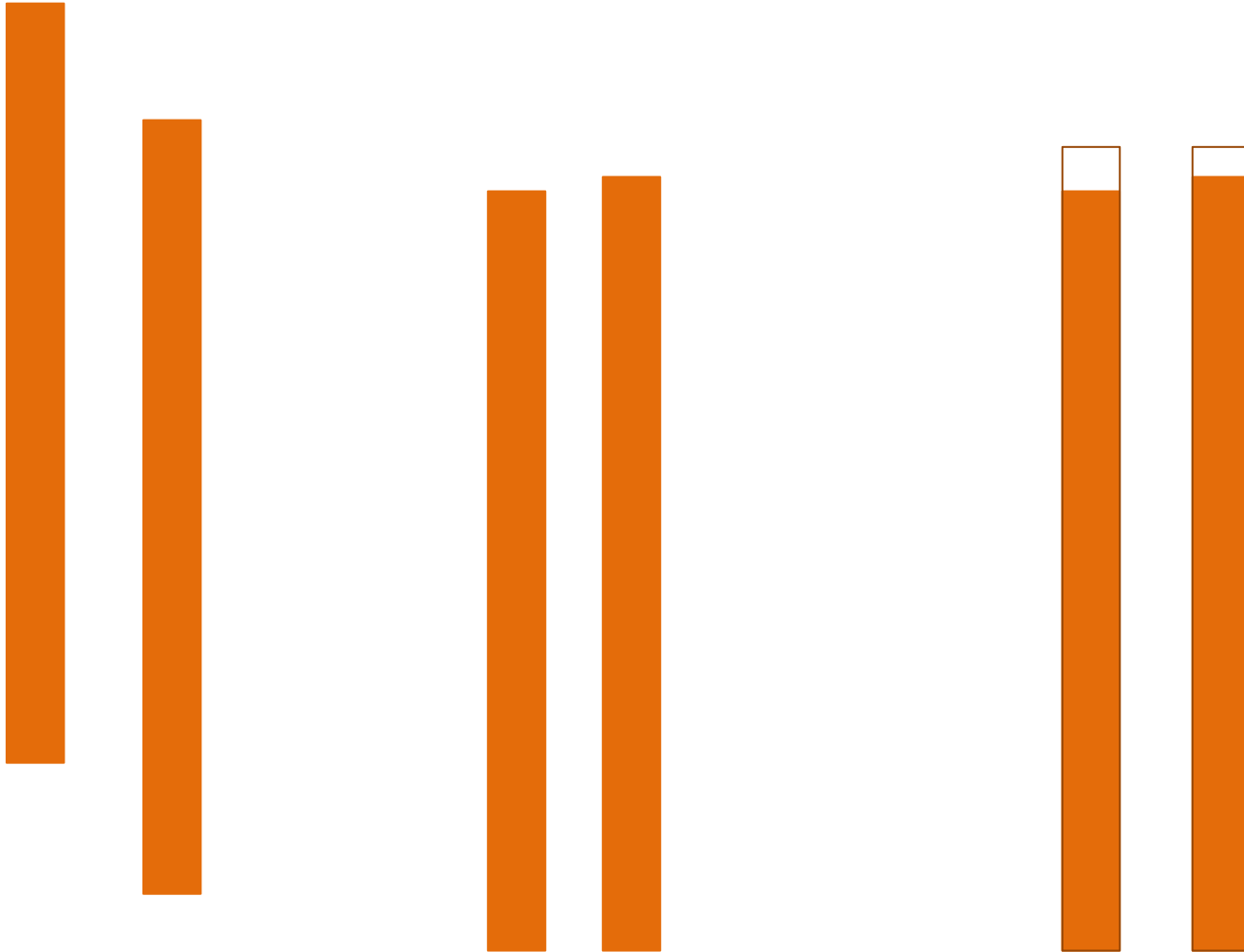
- Where
 - ♦ x : dimension
 - ♦ $d_p(x)$: just noticeable difference
 - ♦ k_p : constant
 - Subjective
 - Environmental

Consequences of Weber's law

- It is easier to compare lengths that differ by a large percentage
- The same difference is easier to notice between smaller measures
 - ◆ More likely to be larger than just noticeable difference

$$x < y \implies d_p(x) < d_p(y)$$

Non-aligned objects lengths



Non-aligned objects lengths

- Additional references my help comparison
 - ◆ They provide alternative possible comparisons
- If lengths range between 0 and a maximum (L), e.g. percentages
- Comparing l_1 and l_2 (close to L) that differ by a small amount d
 - ◆ Difference $L-l_1$ vs. $L-l_2$ easier to notice than l_1 vs. l_2

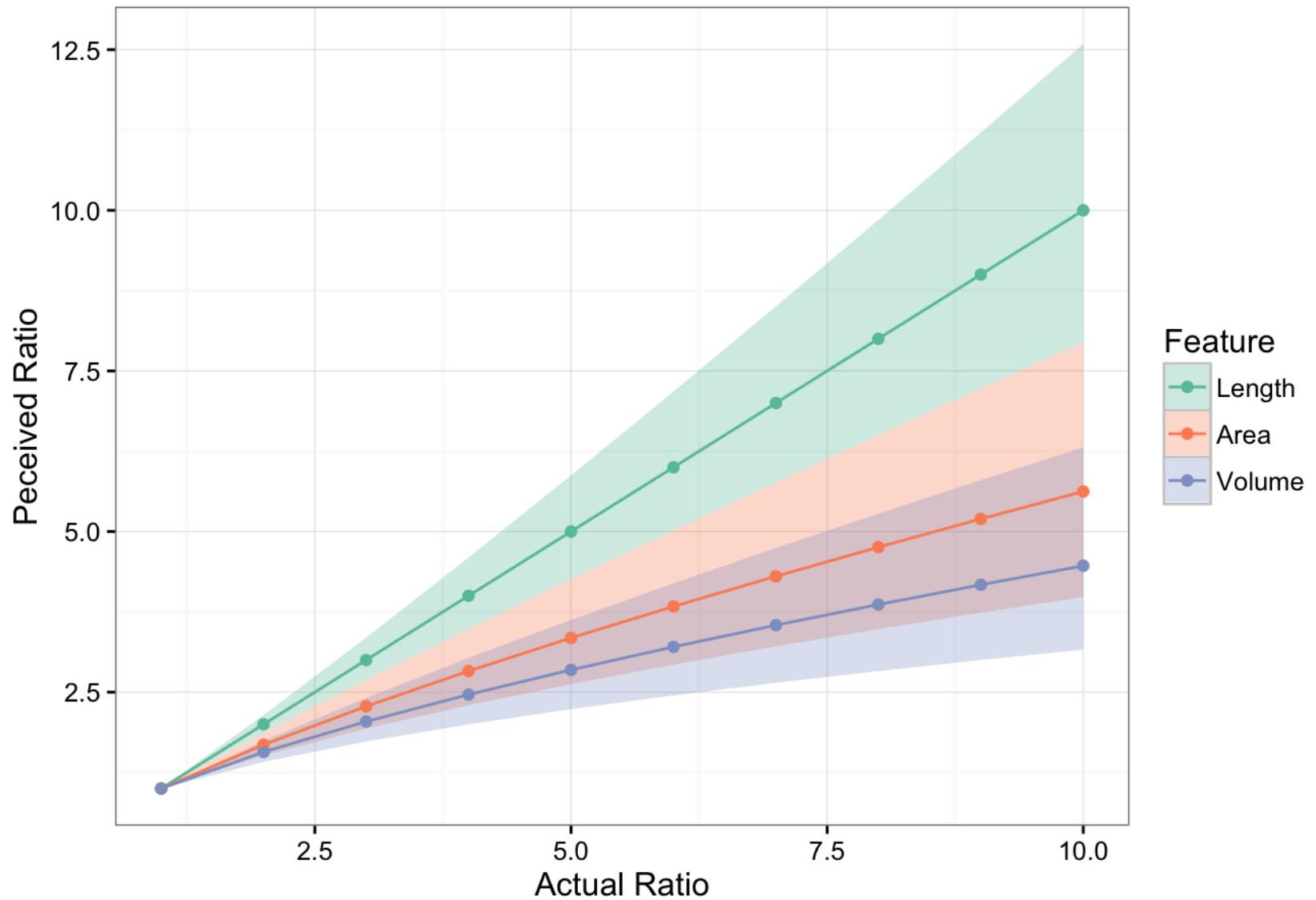
Stevens's law

- Perceive scale (magnitude ratio)

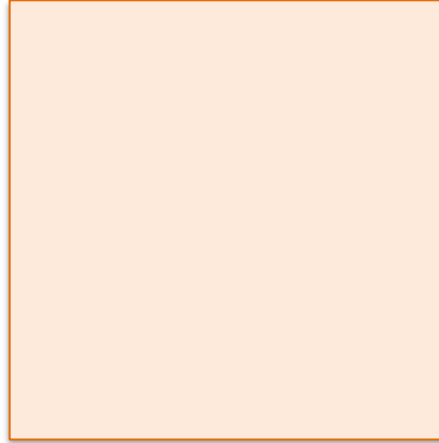
$$p(x) = c \cdot x^{\beta}$$

- Where β depends on spatial dimension
 - ♦ 1D: Length $\rightarrow \beta$ in $[0.9, 1.1]$
 - ♦ 2D: Area $\rightarrow \beta$ in $[0.6, 0.9]$
 - ♦ 3D: Volume $\rightarrow \beta$ in $[0.5, 0.8]$

Steven's law



Steven's law



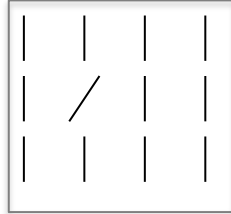
Consequences

- Prefer comparing lengths
- Avoid comparison between areas
 - ◆ Except for ordinal measures
- Never–ever make volume comparisons

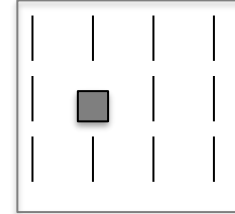
ATTRIBUTES OF FORM

Attributes of form

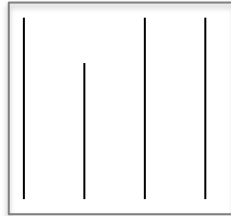
Orientation



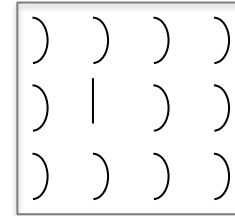
Shape



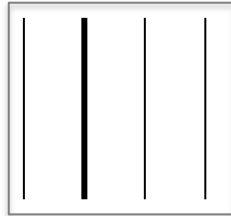
Line Length



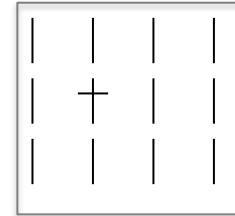
Curvature



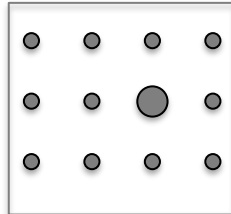
Line Width



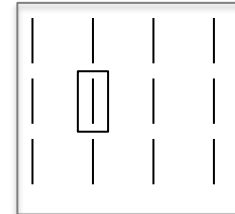
Added mark



Size

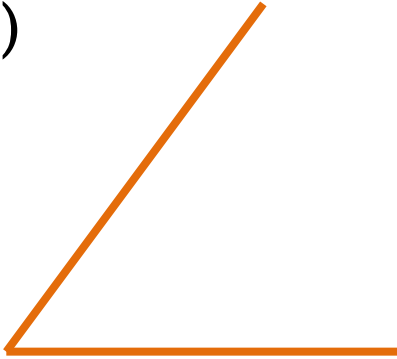


Enclosure

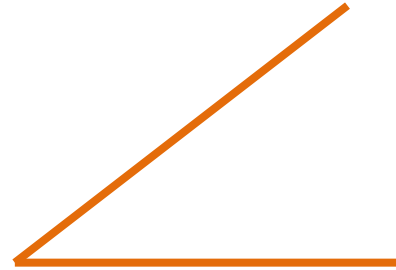


Orientation (angle or slope)

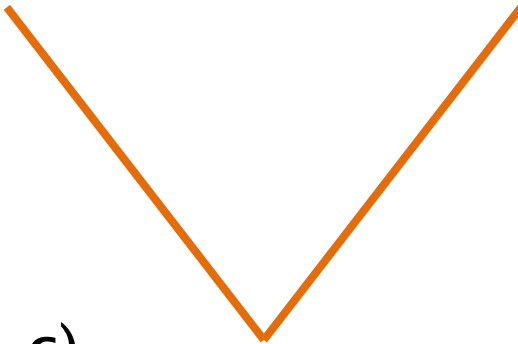
a)



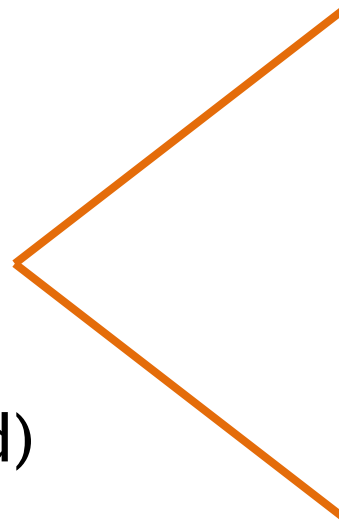
b)



c)

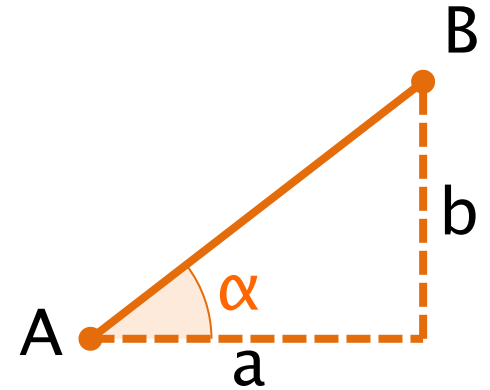


d)



Angle vs. Slope

- Slope of A–B is b/a
 - ♦ $\tan(\alpha)$
- Slope judgment typically falls back to an angle judgment
 - ♦ Given an error ϵ in the angle judgment
 - ♦ It is reflected in a slope error

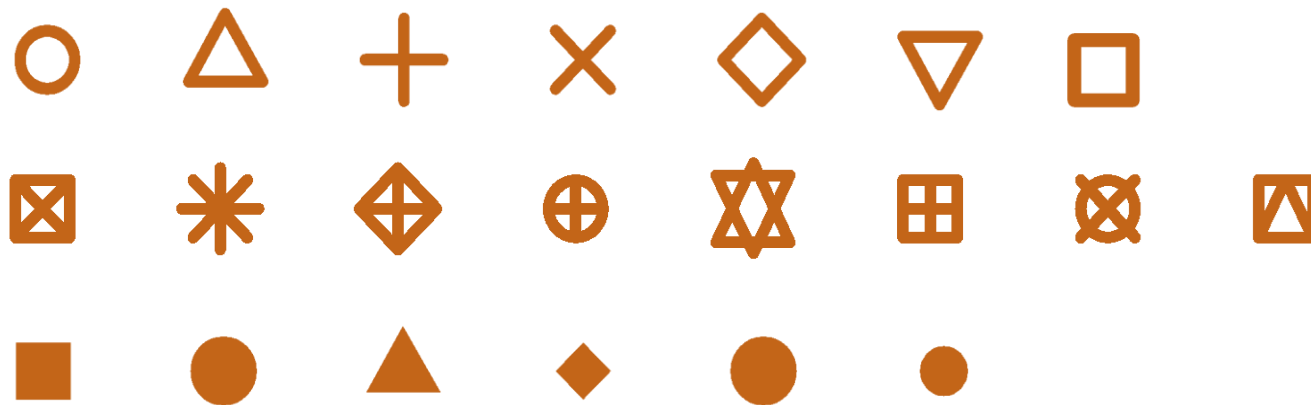


$$\tan(\alpha + \epsilon) - \tan(\alpha) = \epsilon \cdot \tan'(\alpha) = \frac{\epsilon}{\cos^2(\alpha)}$$

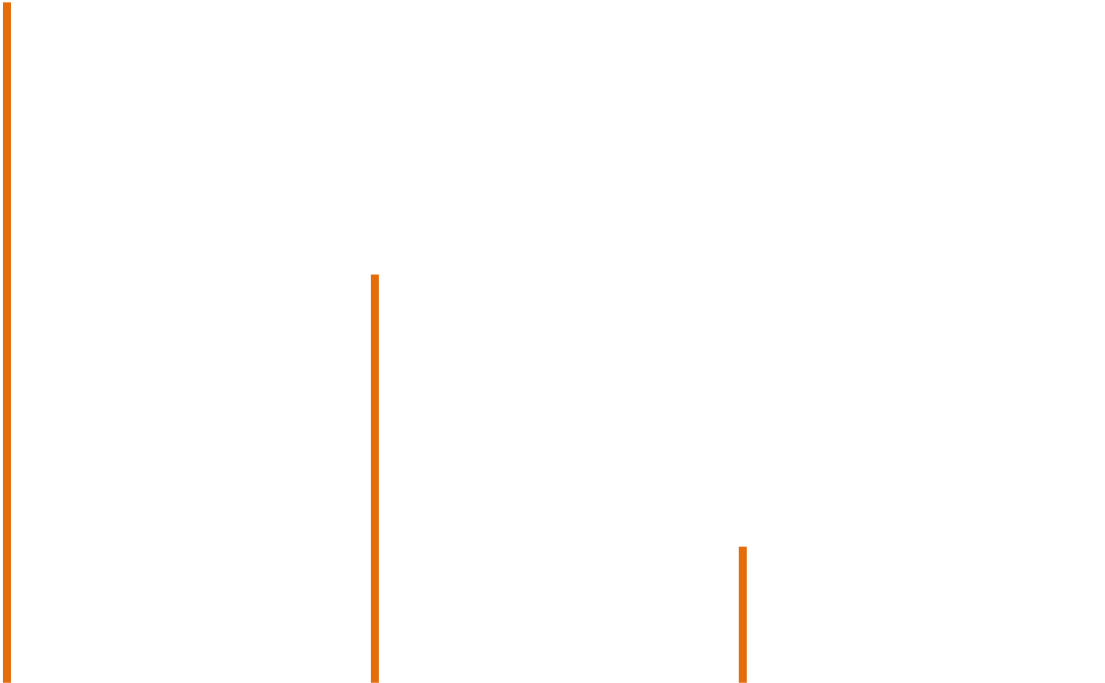
– Getting infinite as α approaches to $\pi/2$

Shape

- There is no common quantitative semantics for the shapes
 - Unless they are characters...
- ◆ Fill textures are shapes too



Length



Effect of context



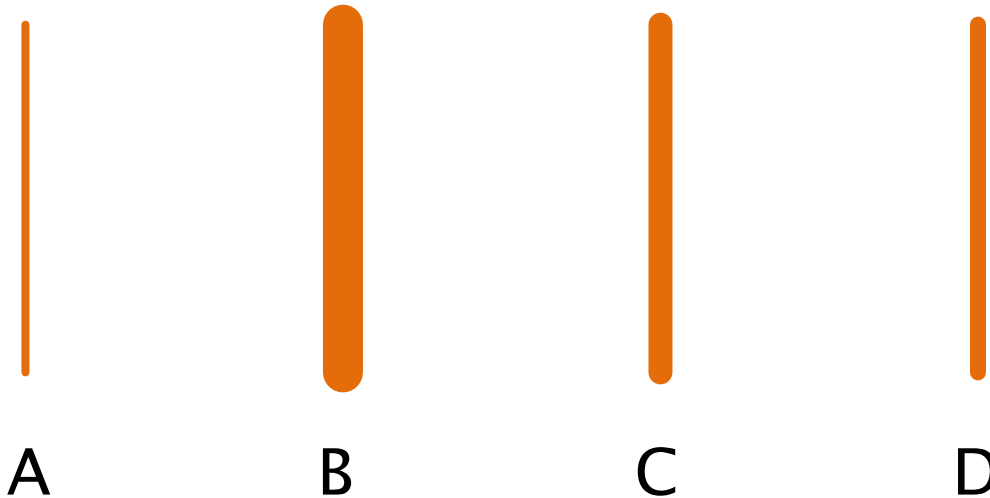
Curvature

- There is no common magnitude assessment for the curvature



Width

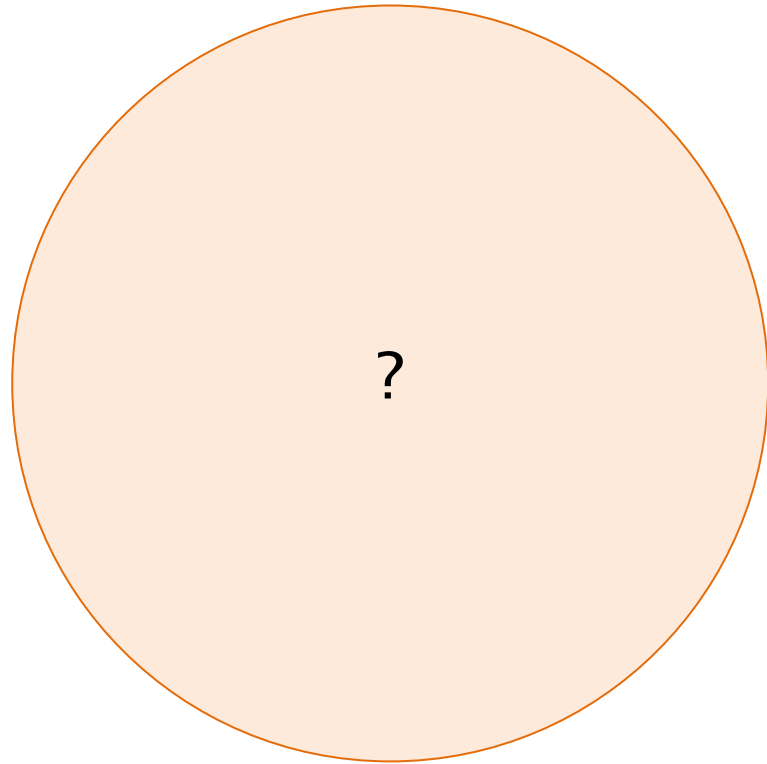
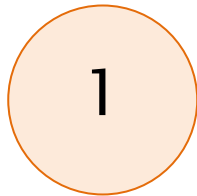
- Order can be identified
 - ◆ Difficult to appreciate actual magnitude



Mark

- No common quantitative semantics of marks
- Number of marks could encode a natural number
 - ♦ Harder to read than a cipher

Size / Area

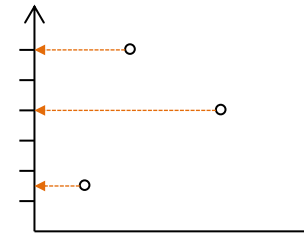


Enclosure

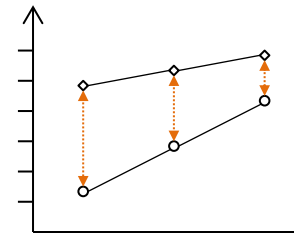
- No common quantitative semantics for enclosure
 - ◆ Except counting items enclosed

Spatial Position

- Position along axis
 - ◆ Common scale
 - ◆ Distinct identical scales
 - Possibly un-aligned

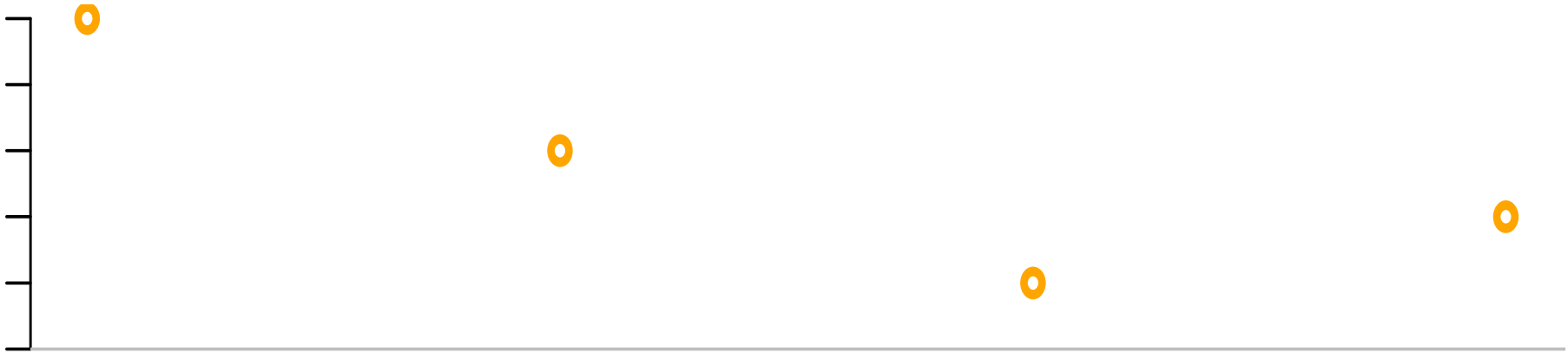


- Distance



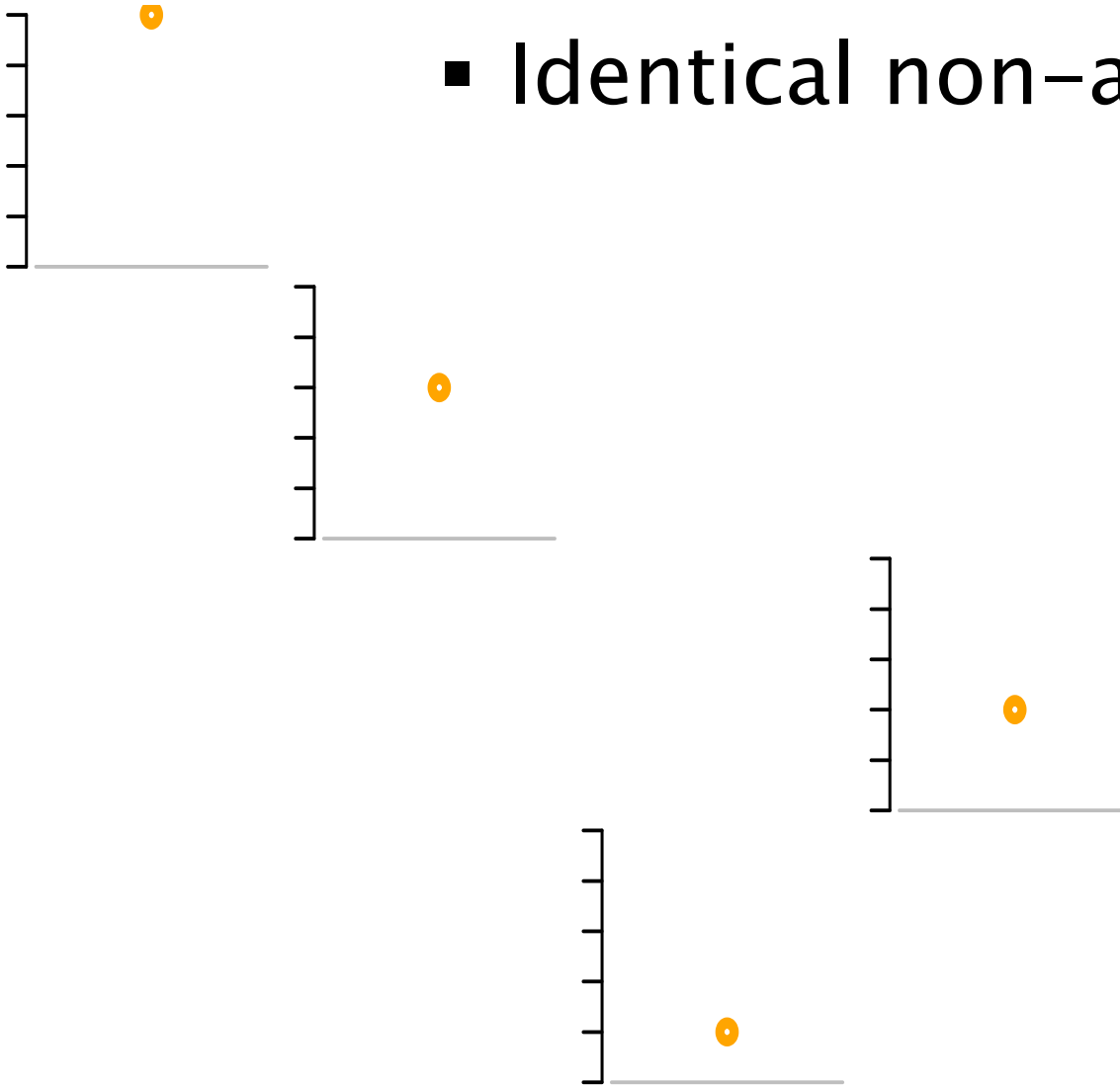
Position

- A common scale



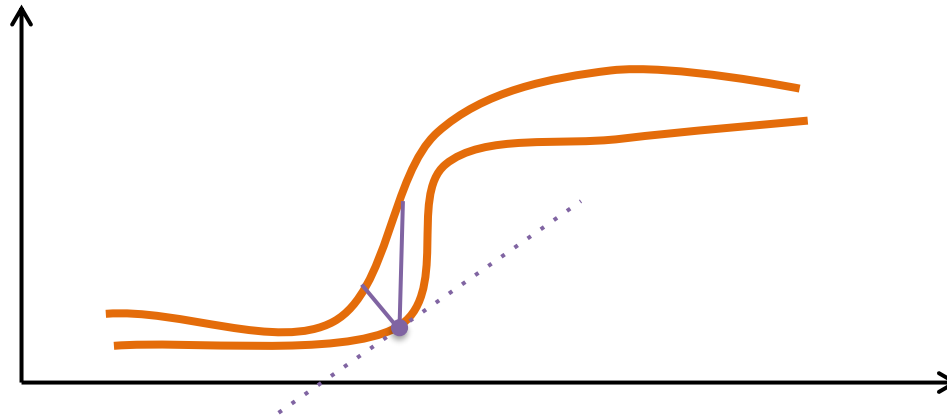
Position

- Identical non-aligned scales



Distance

- Points
 - ◆ Use length of imaginary connecting lines
- Lines
 - ◆ Distance orthogonal to tangent
 - Not what is meant in xy plots



Detection and Separation

Comparison is affected by:

- Detection

- ◆ The capability to visually identify the objects that represent the data to be compared

- Separation

- ◆ The distance between the objects to be compared
 - affects negatively the accuracy

ATTRIBUTE OF COLOR

Attributes of color

- Hue



- Saturation



- Intensity

- ♦ Luminance
- ♦ Value



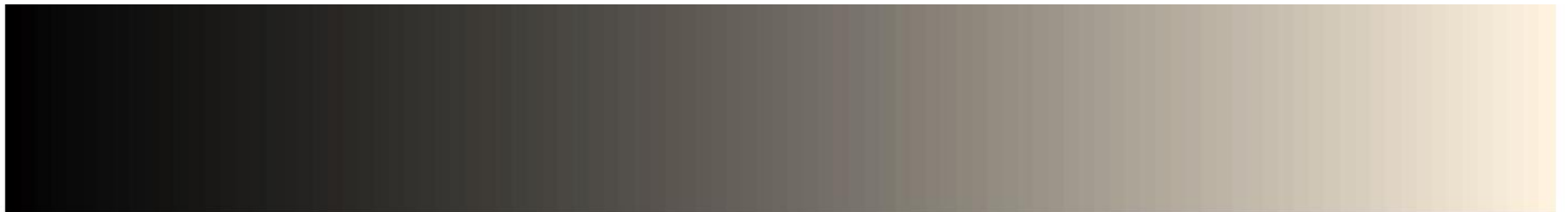
Hue

- There is no common ordering semantics for hues
 - ◆ High spatial frequencies are perceived through intensity changes
 - ◆ Often perceived as separated into bands of almost constant hue, with sharp transitions between hues
- Nominal values can be represented by suitably spaced values



Intensity

- ♦ a.k.a. Luminance, Value
- Provides a perceptually unambiguous ordering
 - ♦ Context can affect accuracy



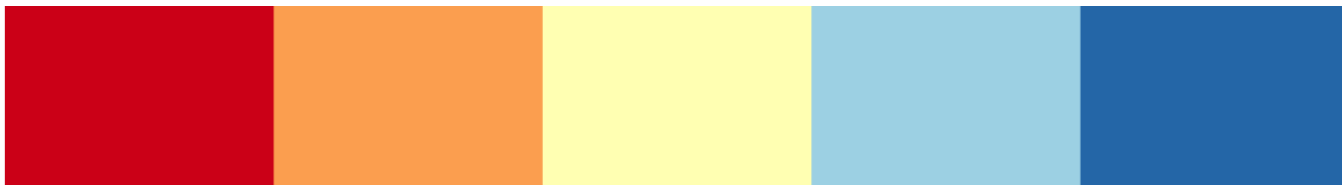
Saturation

- Perceptually difficult to associate an ordered semantics
 - ◆ Can be combined with hue to increase discrimination



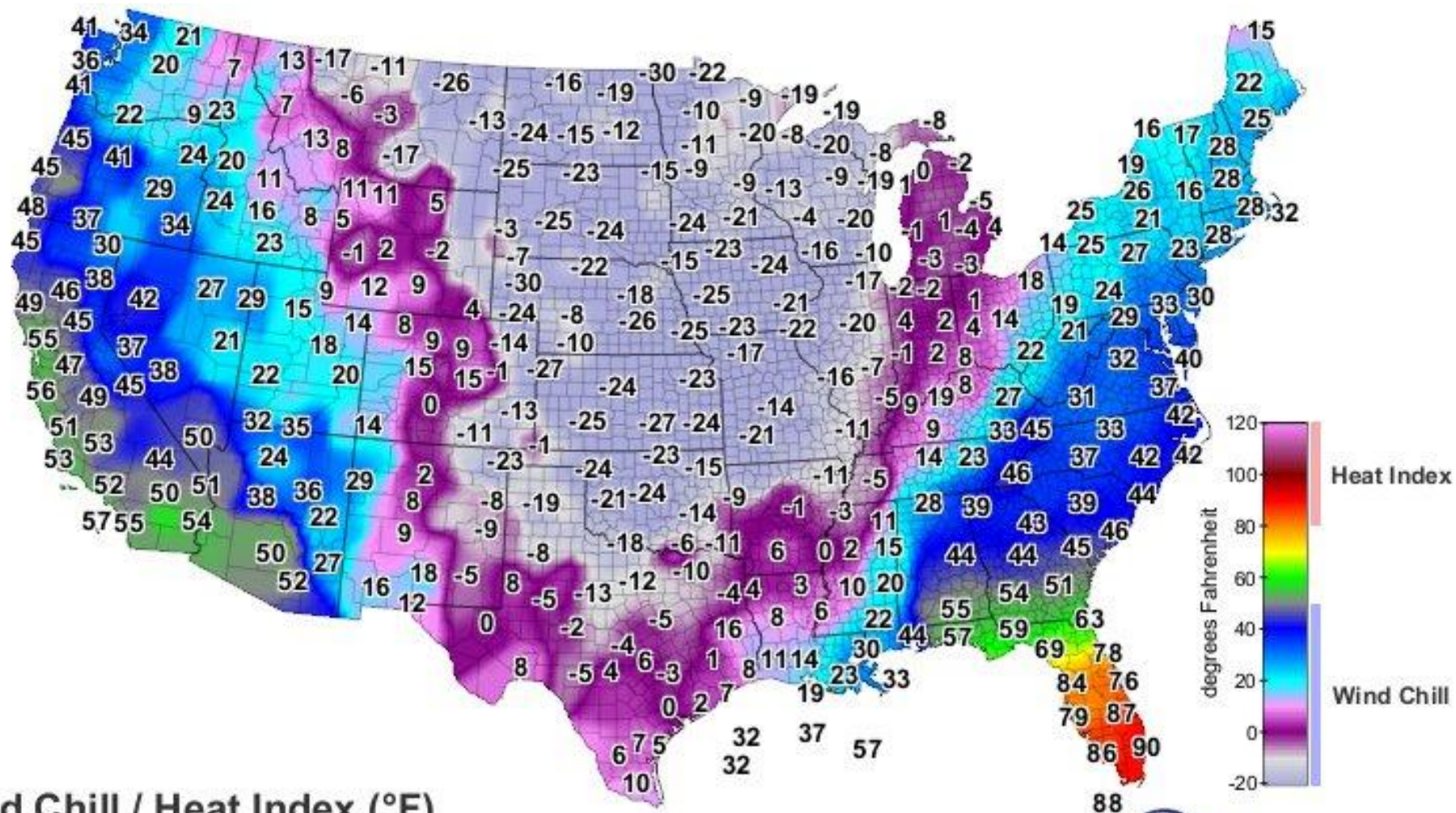
Color usage

- Ordinal measure should be mapped to increasing saturation **and** intensity
 - ♦ Avoid rainbow palette
- Use sequential or diverging palette
 - ♦ E.g.



– <http://colorbrewer2.org/>

Rainbow palette



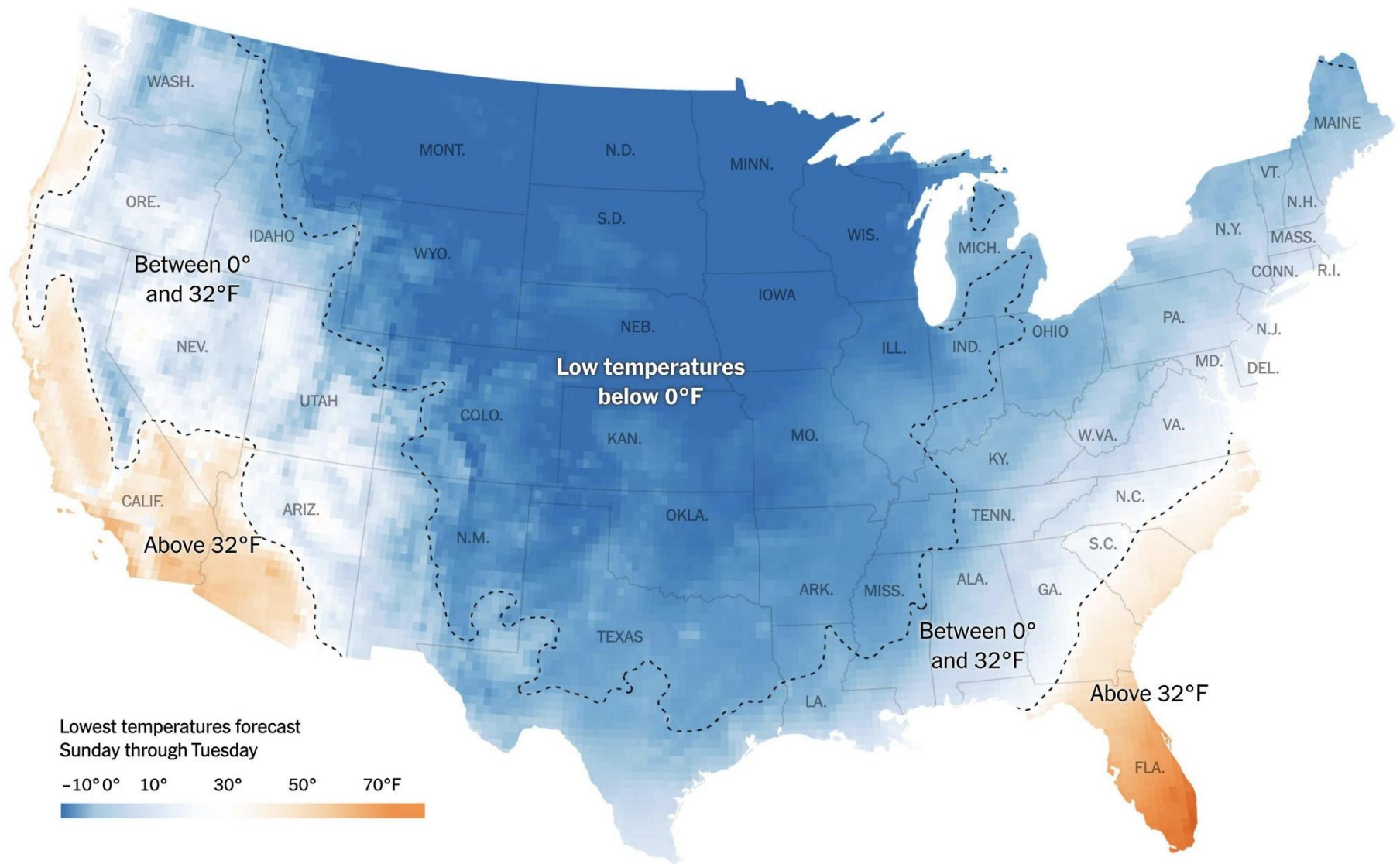
Wind Chill / Heat Index (°F)

11:00 AM February 15, 2021 CST

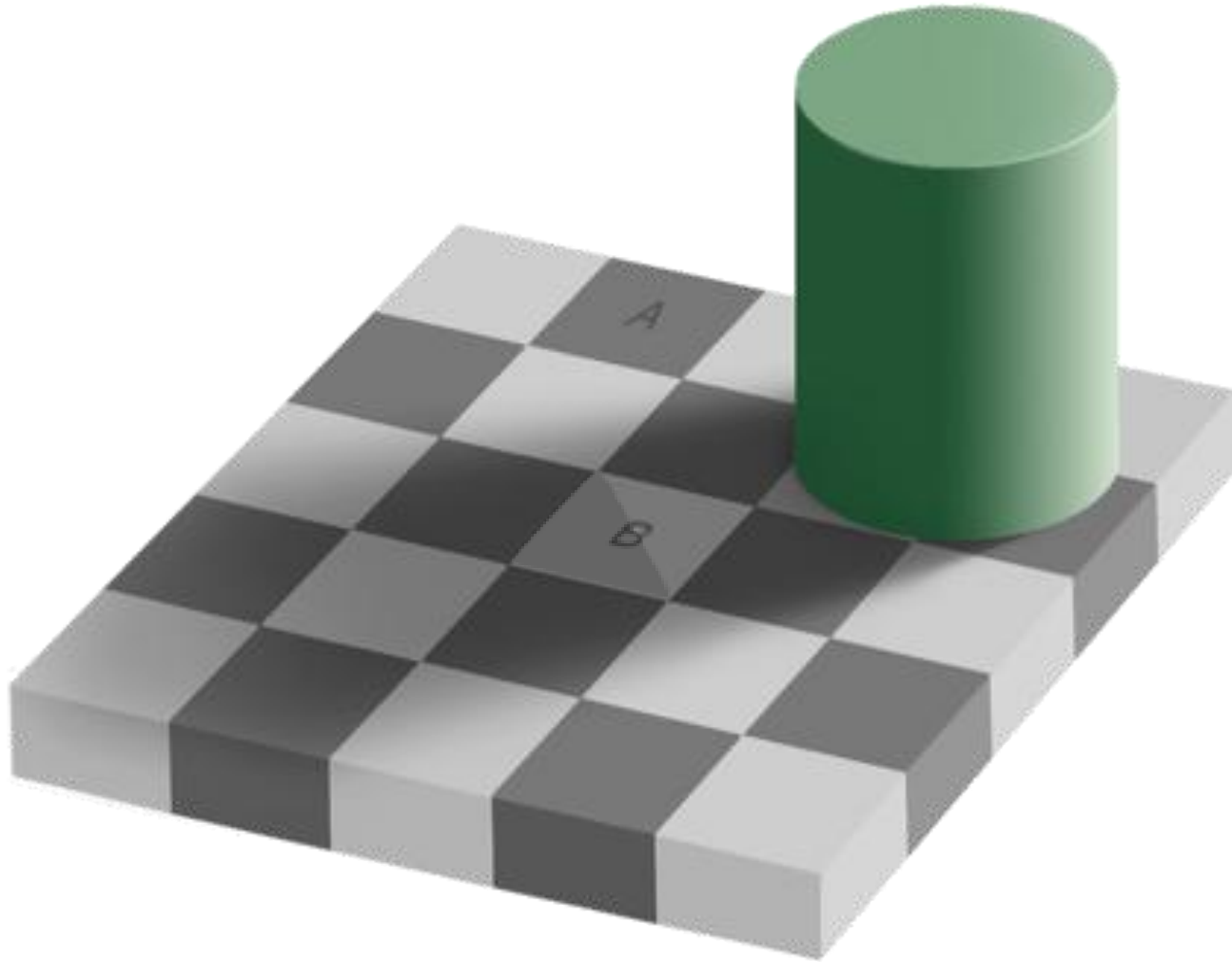
Data provided by NOAA's National Weather Service. Created 11:10:34 AM February 15, 2021 CST. © Copyright 2021



Gradient palette



Effect of Context

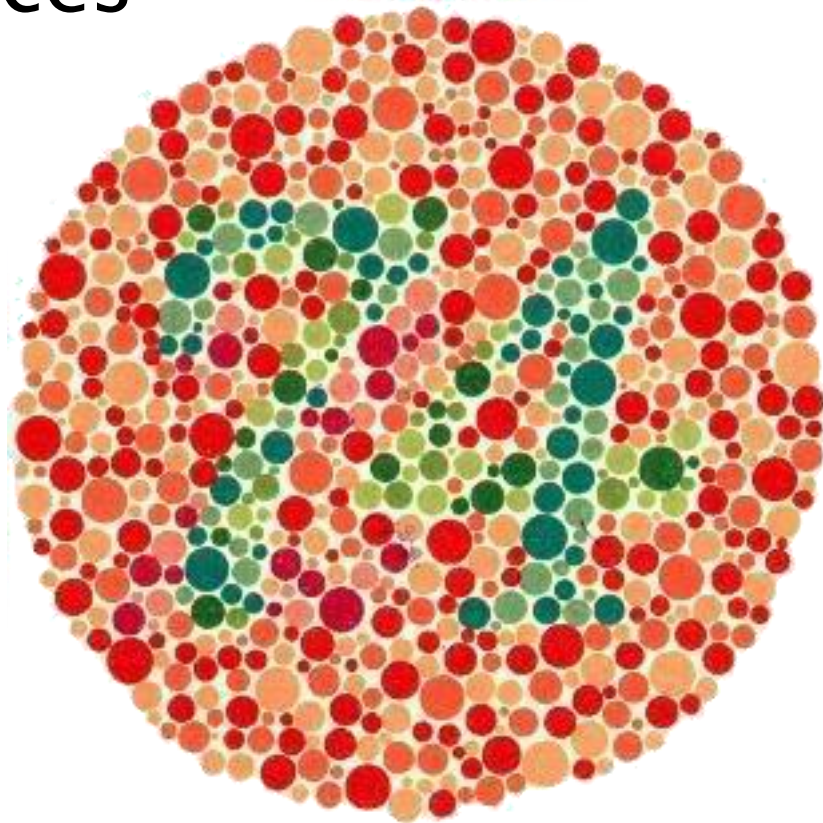


Effect of Context

- Use uniform background
 - ◆ To make distinct visual objects for the same feature look the same
- Use a background color that is contrasting enough with the visual objects' color
 - ◆ To make visual objects easily seen
- Avoid non-uniform background

Color Blindness

- Inability to see colors or perceive color differences

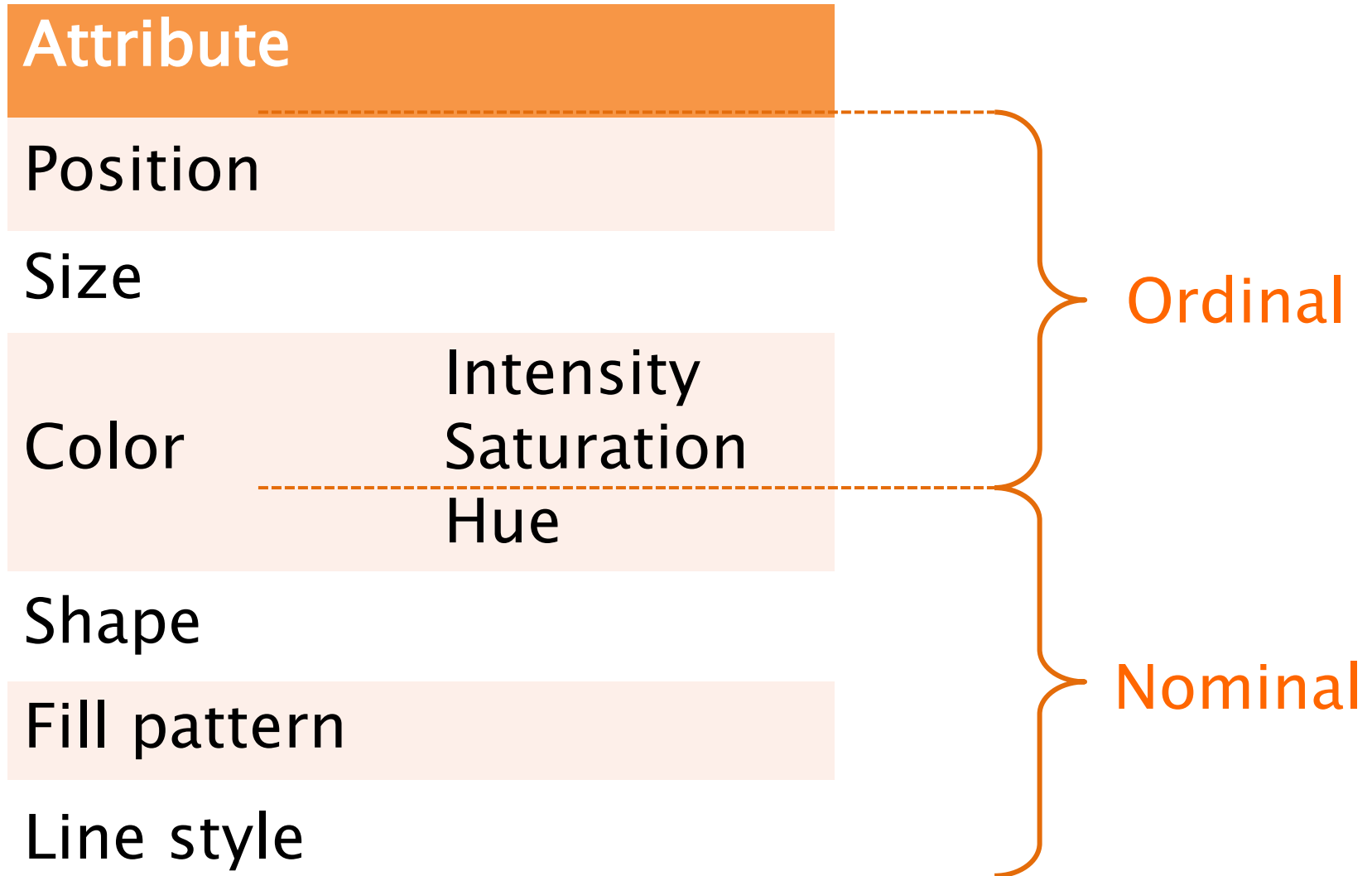


<http://www.color-blindness.com>

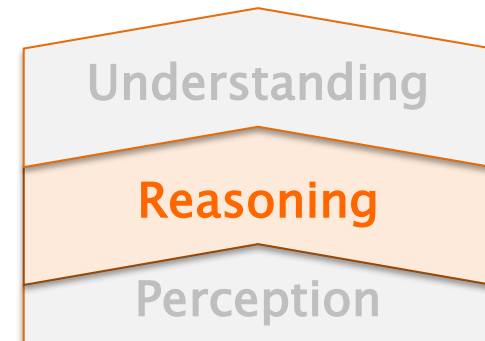
Visual Encoding: Quantitative

Object	Attribute
Point	Position (w.r.t. axis/axes)
Line	Length Position (w.r.t. axis/axes) Slope
Bar	Length
Shape	Size (area) Count

Visual Encoding: Categorical



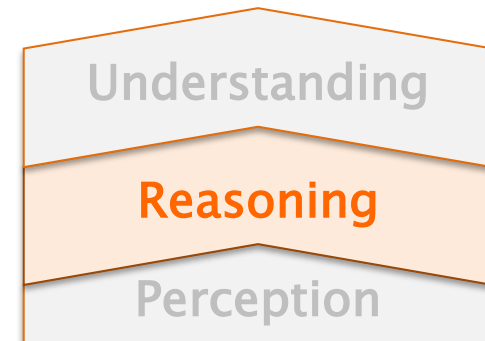
VISUAL REASONING



Graph layout

Layout + visual attributes should allow:

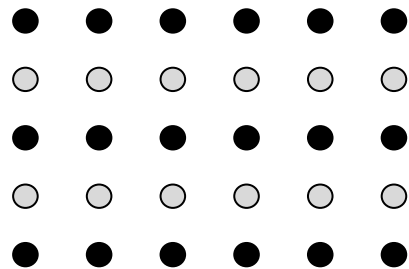
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 - ◆ Distinguish visual objects or group of –
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- **Magnitude assessment**
 - ◆ Evaluate the (relative) magnitude of visual objects



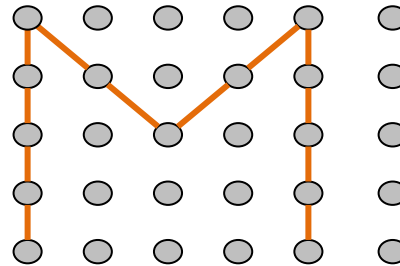
Gestalt principles

- Visual features that lead the viewer to group visual objects together

Similarity



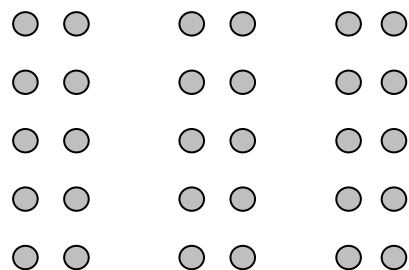
Connection



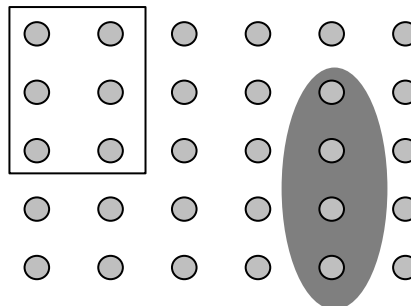
Closure



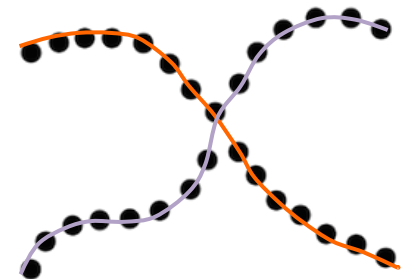
Proximity



Enclosure



Continuity



Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ Enclosure
 - ◆ Closure
 - ◆ Continuity
 - ◆ Connection

Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate

- ◆ Proximity

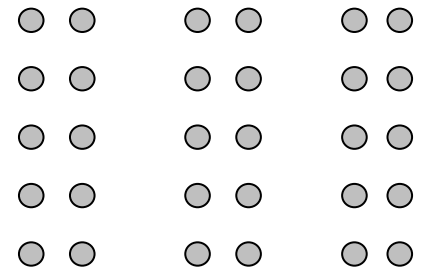
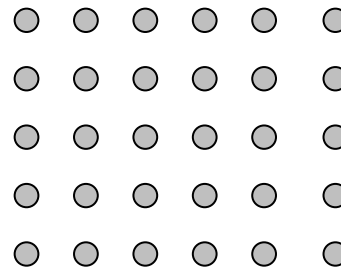
- ◆ Similarity

- ◆ Enclosure

- ◆ Closure

- ◆ Continuity

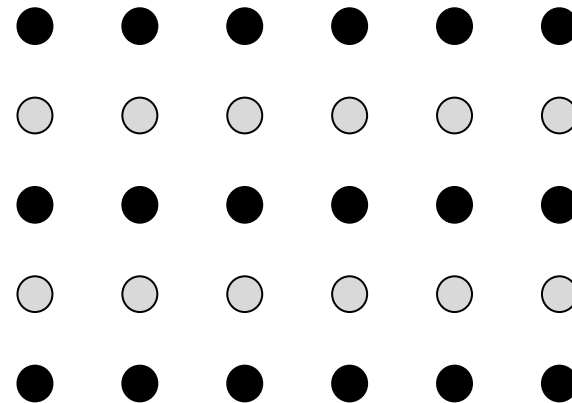
- ◆ Connection



Gestalt principles

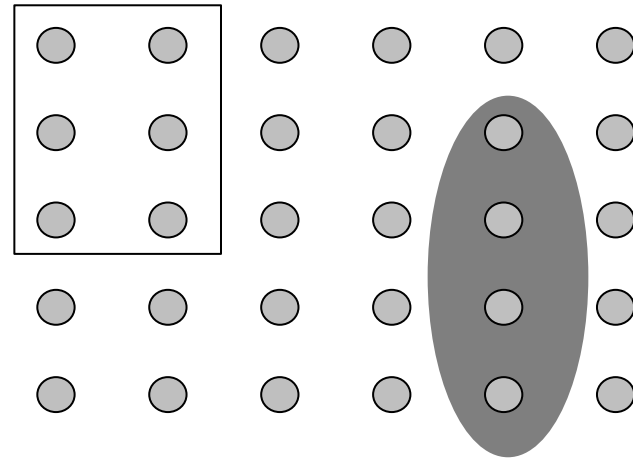
- Visual patterns that lead observers to perceive objects together or separate

- ◆ Proximity
- ◆ **Similarity**
- ◆ Enclosure
- ◆ Closure
- ◆ Continuity
- ◆ Connection



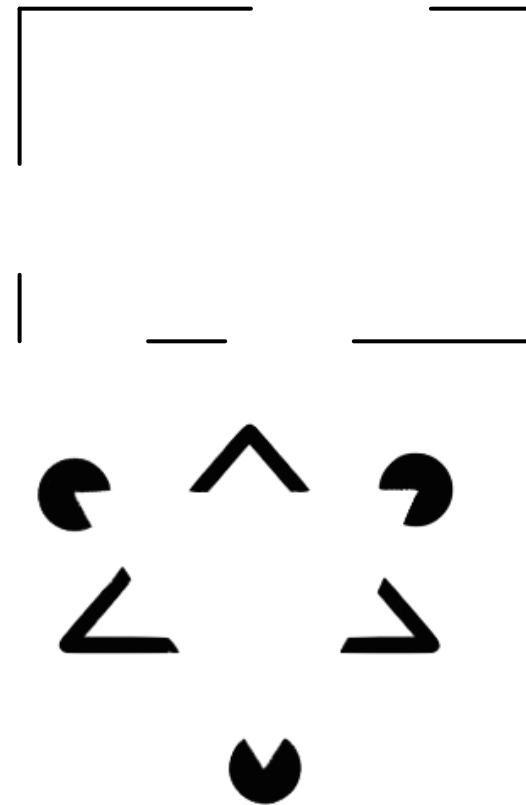
Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ **Enclosure**
 - ◆ Closure
 - ◆ Continuity
 - ◆ Connection



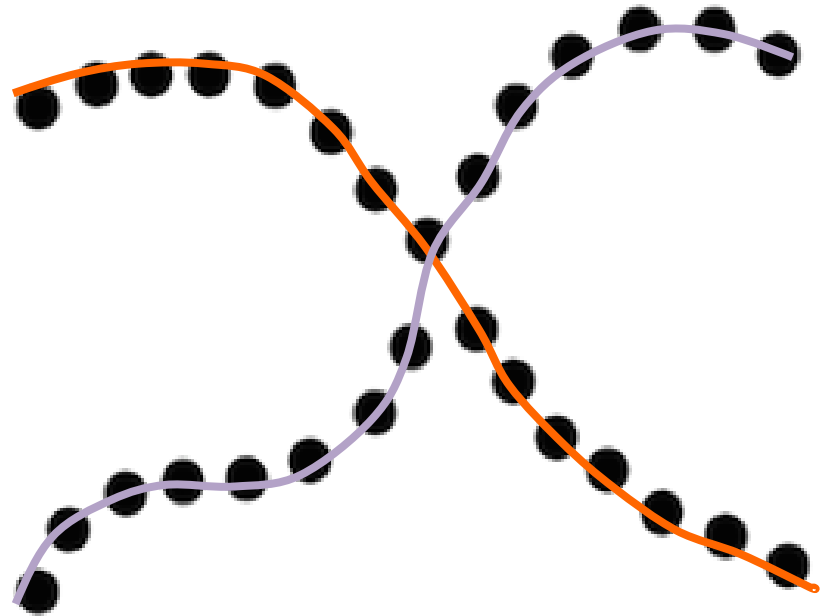
Gestalt principles

- Visual patterns that lead observers to perceive objects together or separate
 - ◆ Proximity
 - ◆ Similarity
 - ◆ Enclosure
 - ◆ **Closure**
 - ◆ Continuity
 - ◆ Connection



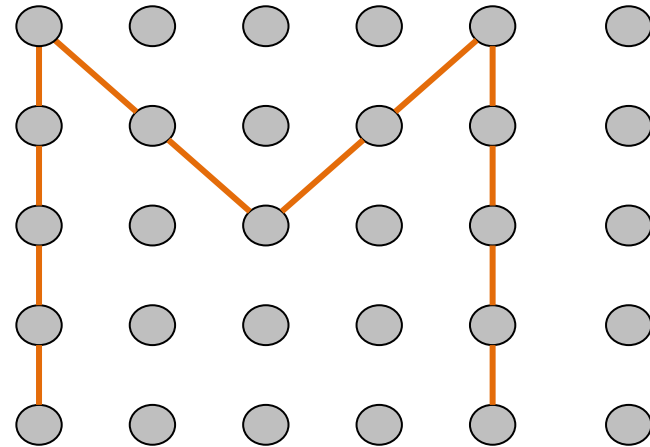
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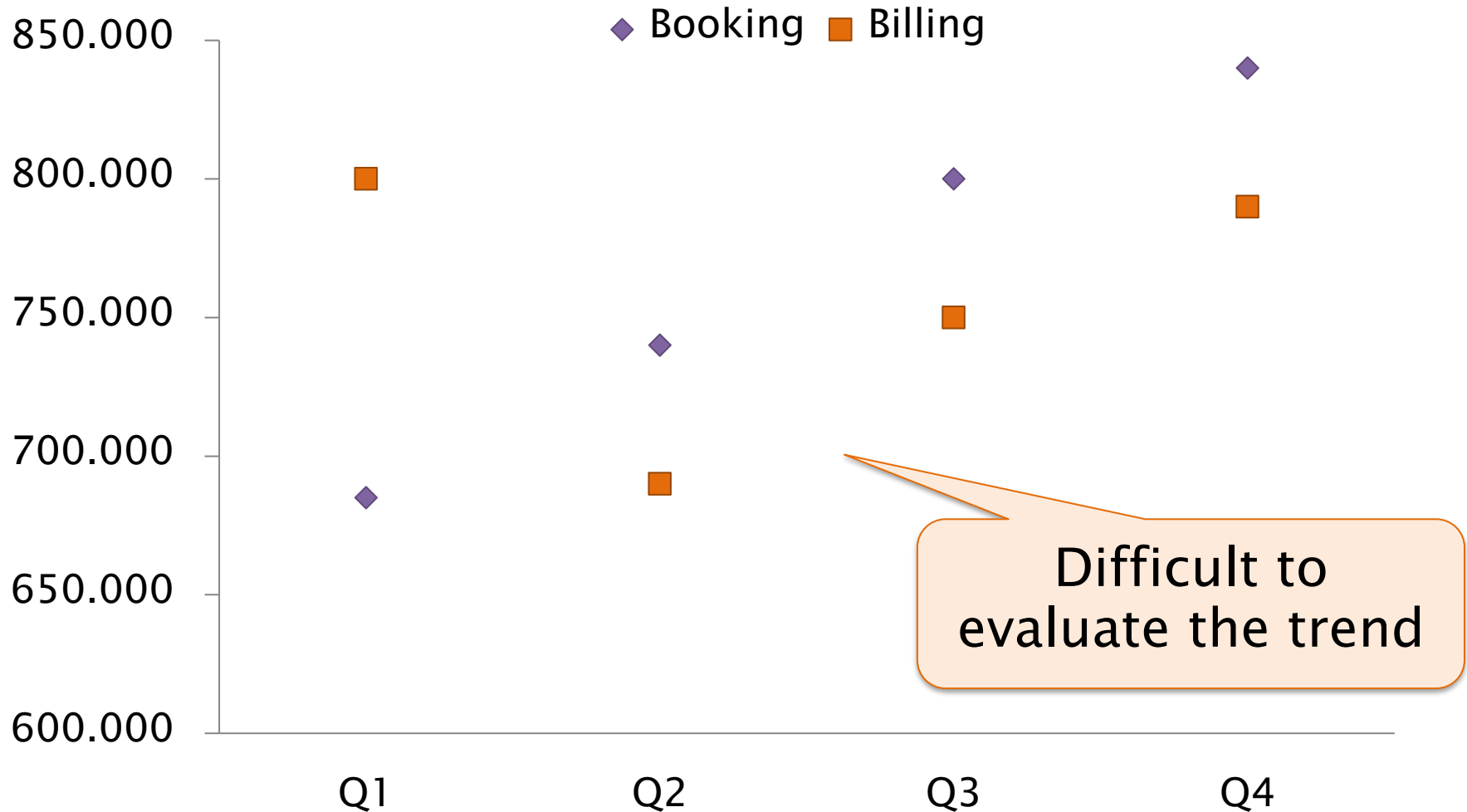


Gestalt principles

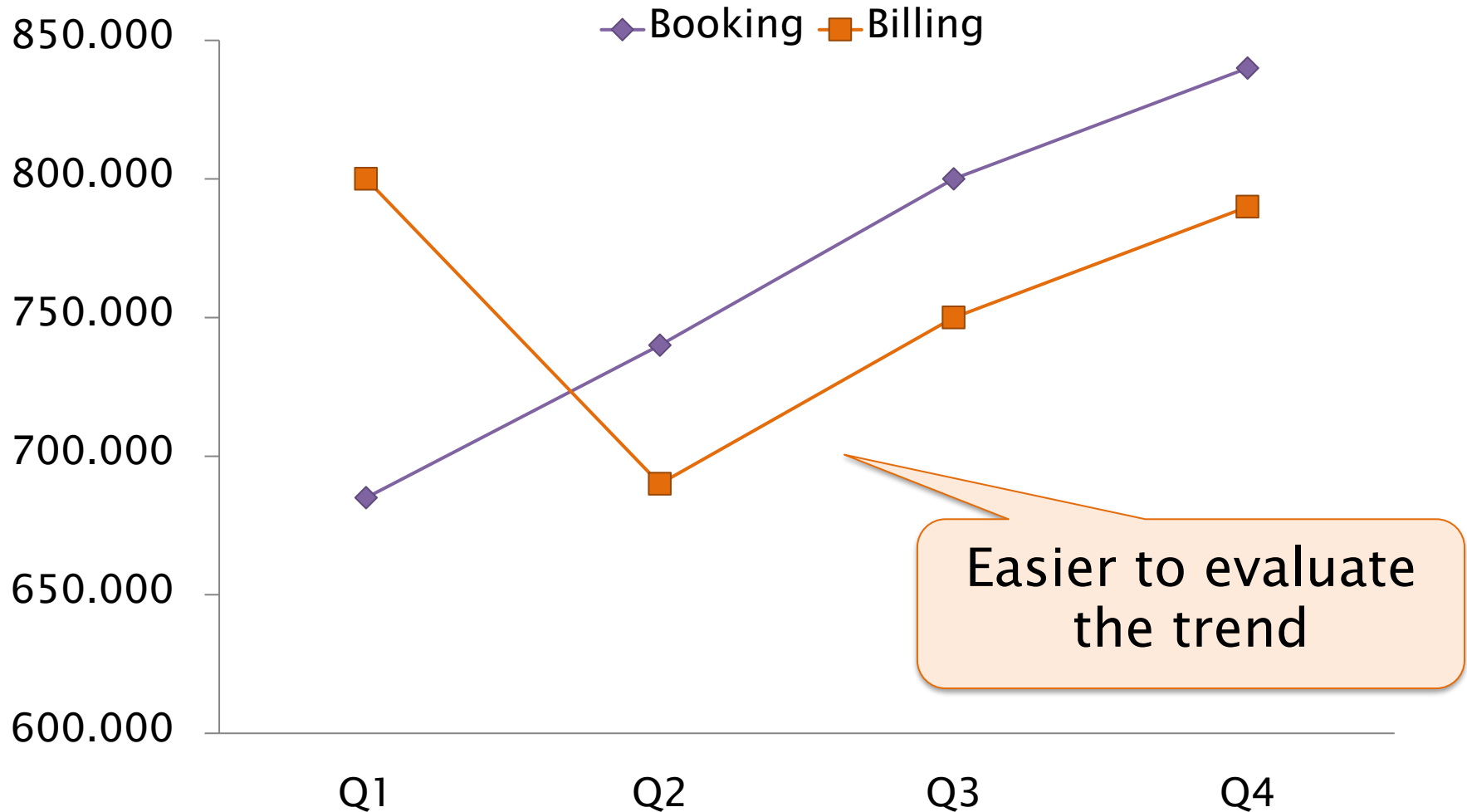
- Visual patterns that lead observers to perceive objects together or separate
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 - ◆ **Connection**



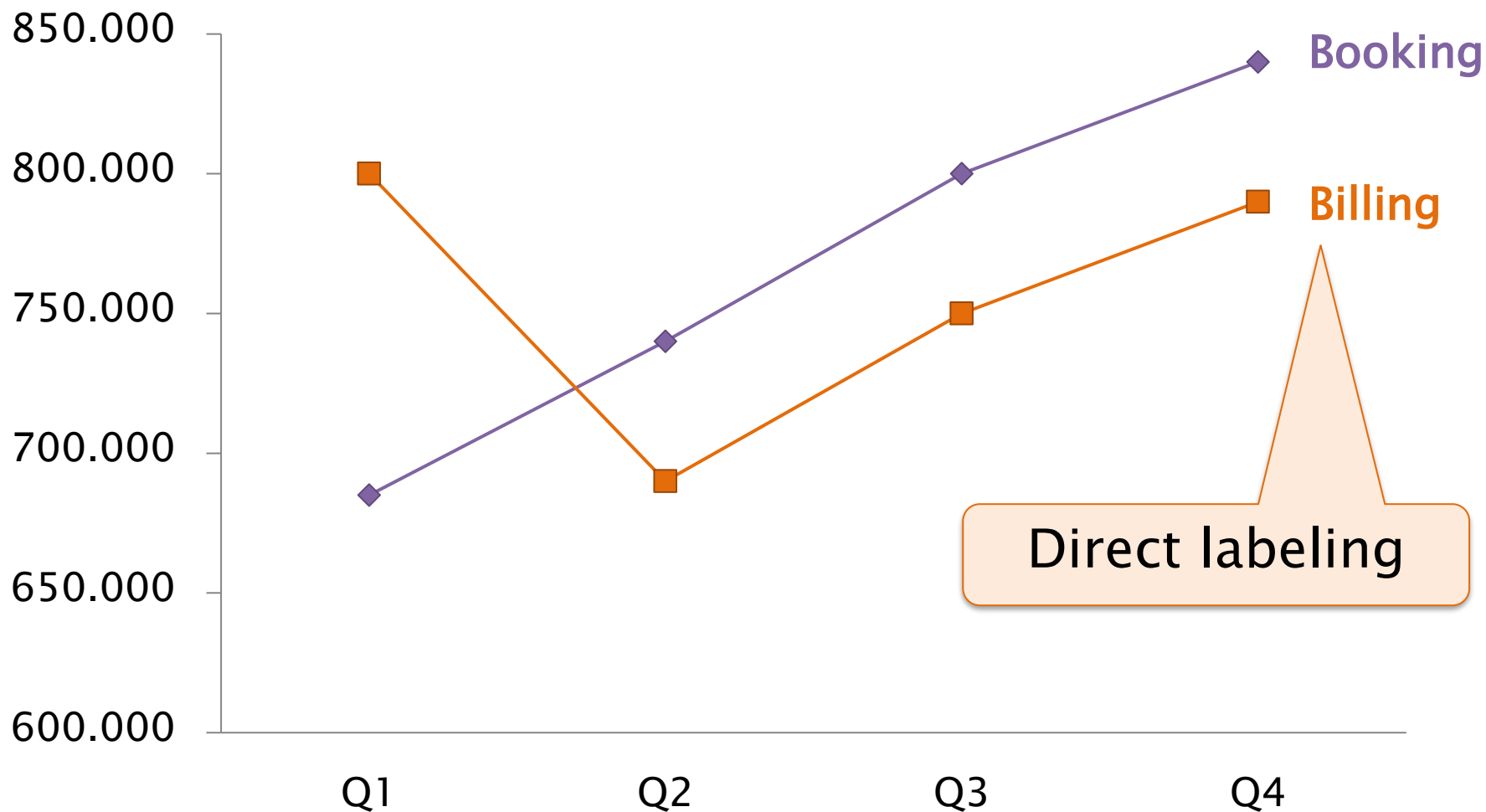
Similarity in Shape & Color



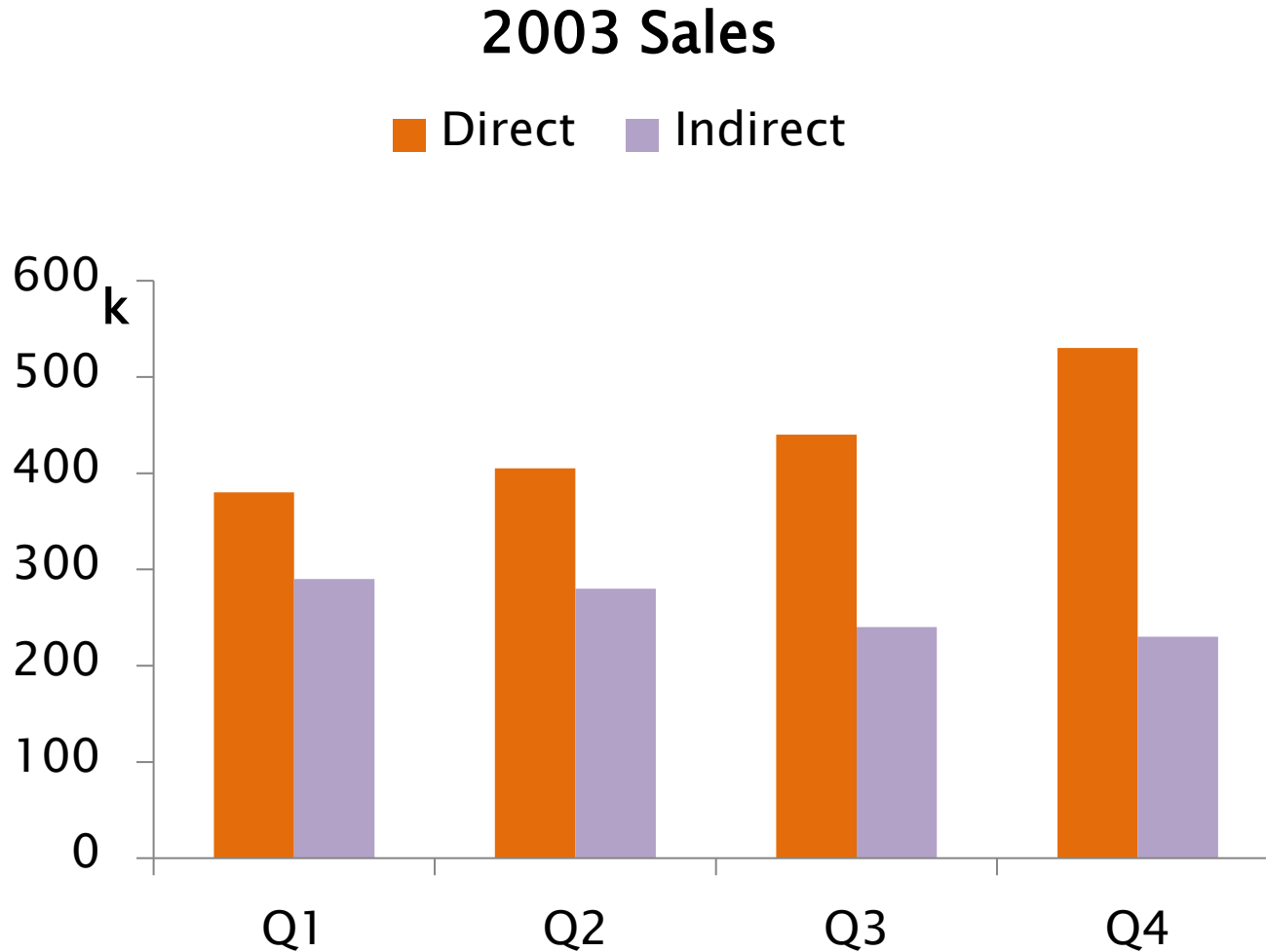
Similarity+Connection



Similarity+Connection+Proximity



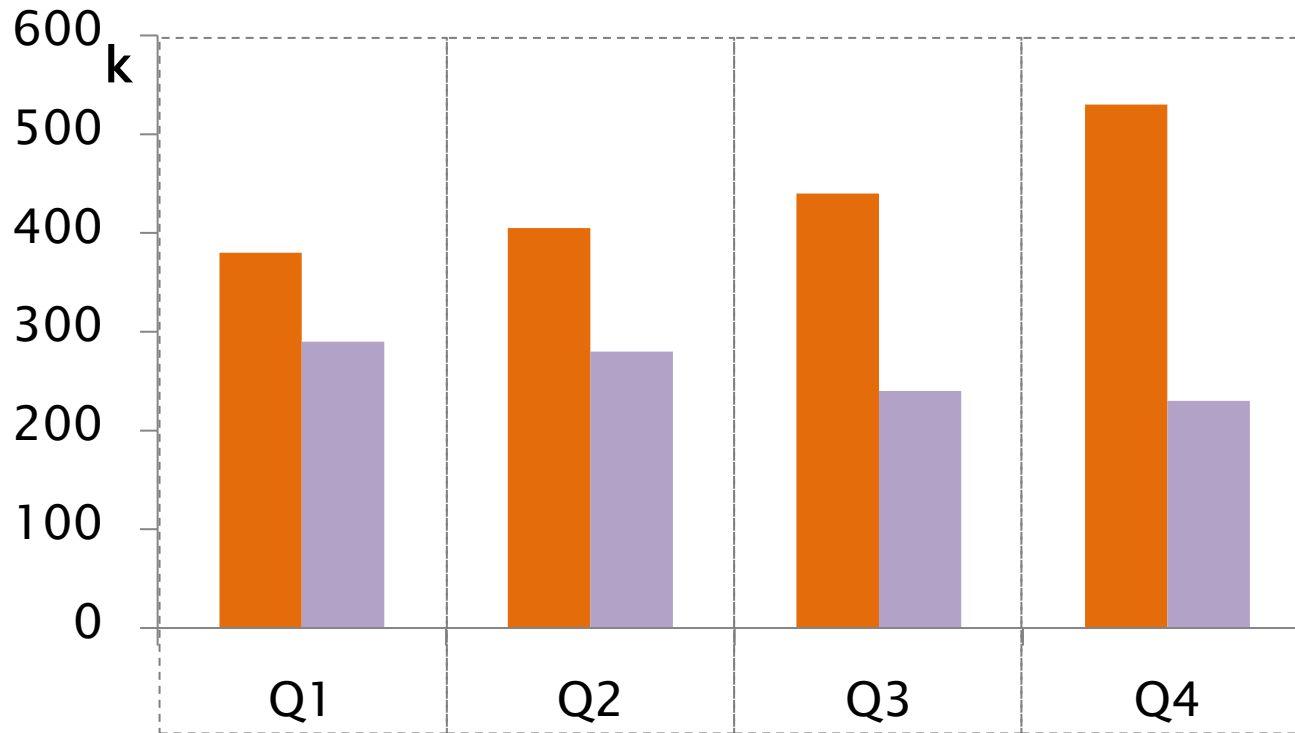
Similarity $\times$ Proximity



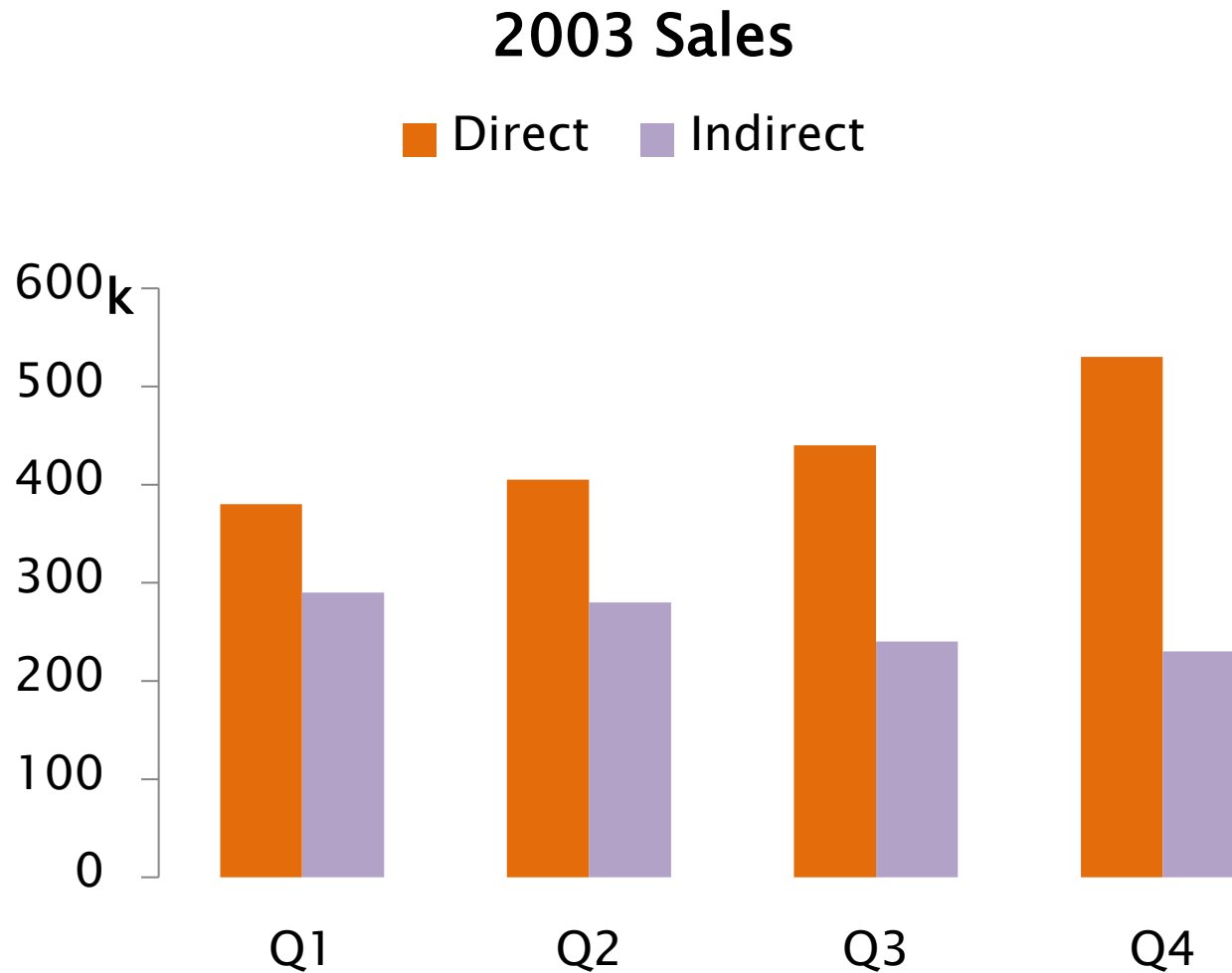
Similarity $\times$ Proximity & Enclosure

2003 Sales

Direct Indirect



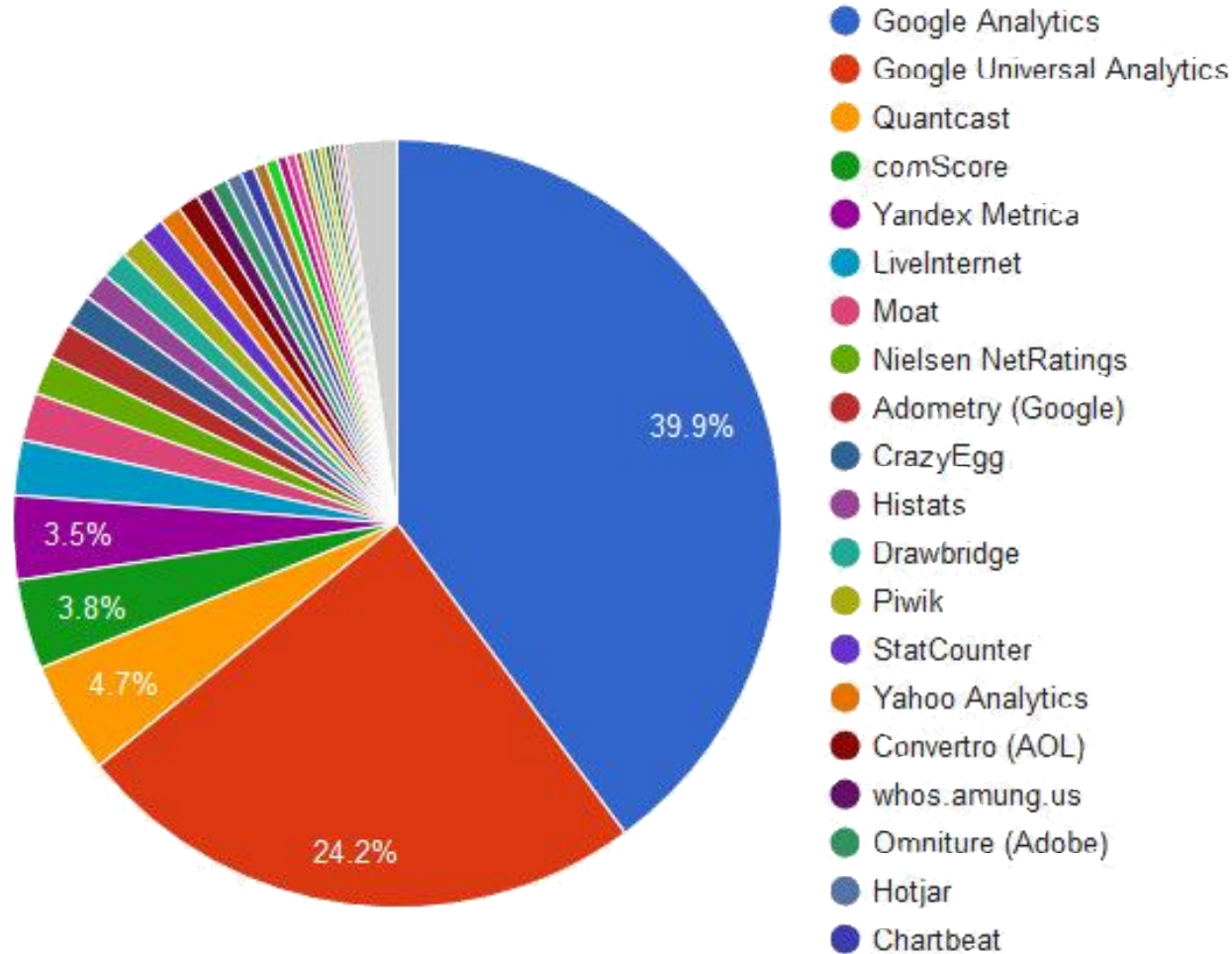
Continuity replaces axis



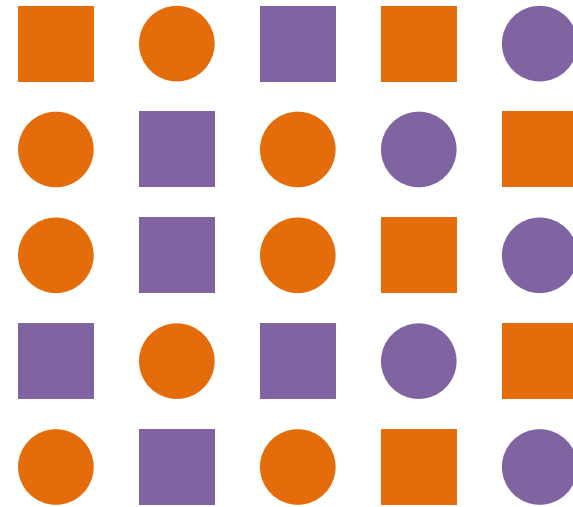
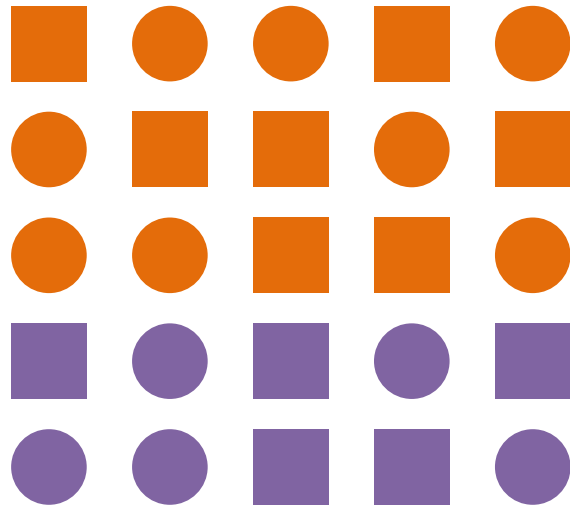
Distinct perceptions

- The immediacy of any pre-attentive cue declines as the variety of alternative patterns increases
 - ◆ Even if all the distracting patterns are individually distinct from the target
 - ◆ For each single attribute no more than **four** distinct levels are immediately discernible
 - ◆ This limit affects the similarity principle

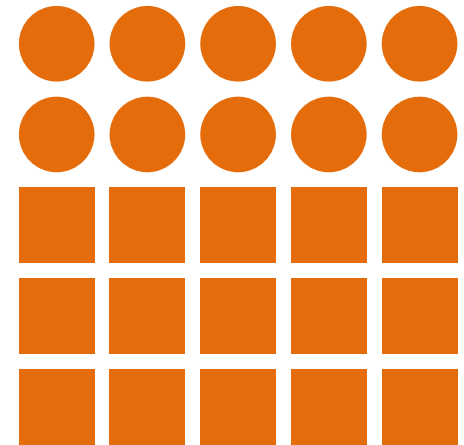
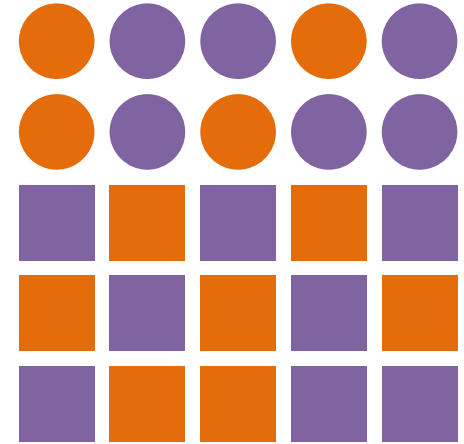
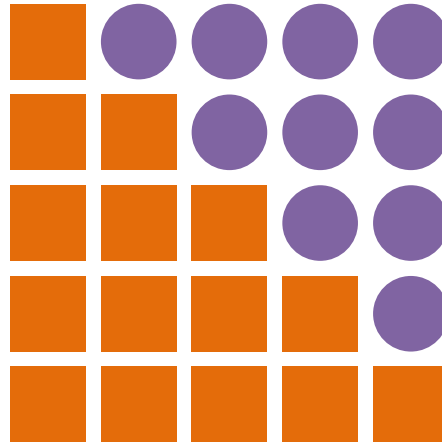
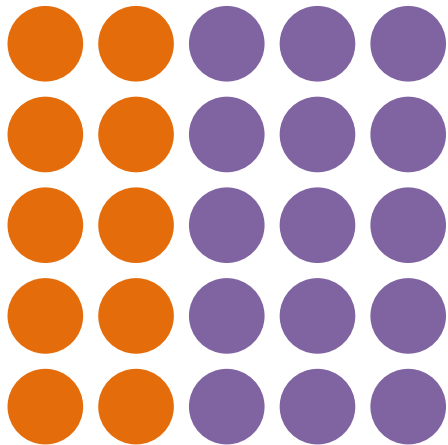
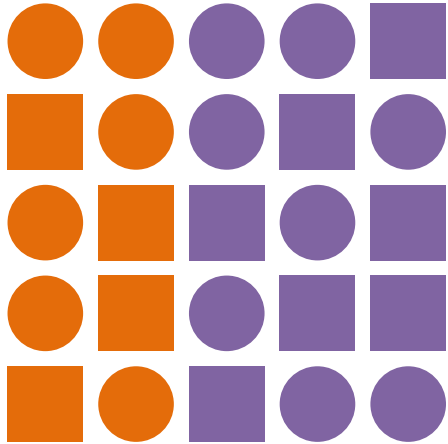
Rainbow Pies



Attribute Interference



Attribute Interference



Cultural conventions

- Reading proceed from left to right and from top to bottom
 - ◆ At least in western culture
- What is at the top (on the left) precedes what is at the bottom (on the right) in terms of
 - ◆ Importance
 - ◆ Ordering
 - ◆ Time

Emphasis

Attribute	Tables	Graphs
Line width	Boldface text	Thicker lines
Size	Bigger tables Larger fonts	Bigger graphs Wider bars Bigger symbols
Color intensity	Darker or brighter colors	
2-D position	Positioned at the top Positioned at the left Positioned in the center	

Visualizzazione dell'Informazione Quantitativa

VISUAL INTEGRITY

- **Proportionality**

- ◆ Representation as physical quantities should be proportional to the represented numbers

- **Utility**

- ◆ Graphical element should convey useful information

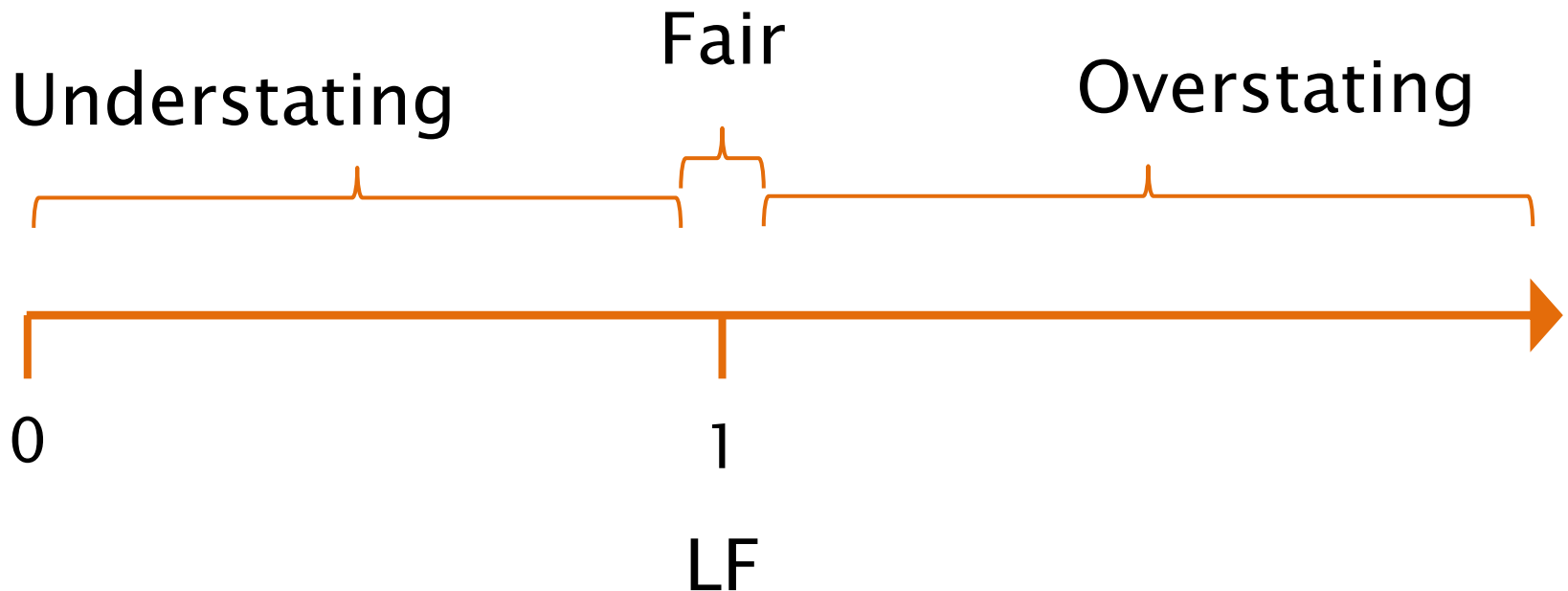
- **Clarity**

- ◆ Labeling should counter graphical distortion and ambiguity

- The magnitude of visual attributes should represent faithfully the magnitude of measures
- They should allow
 - ◆ Discrimination: are they different?
 - ◆ Comparison: which is larger?
 - ◆ Magnitude Assessment: how much larger?

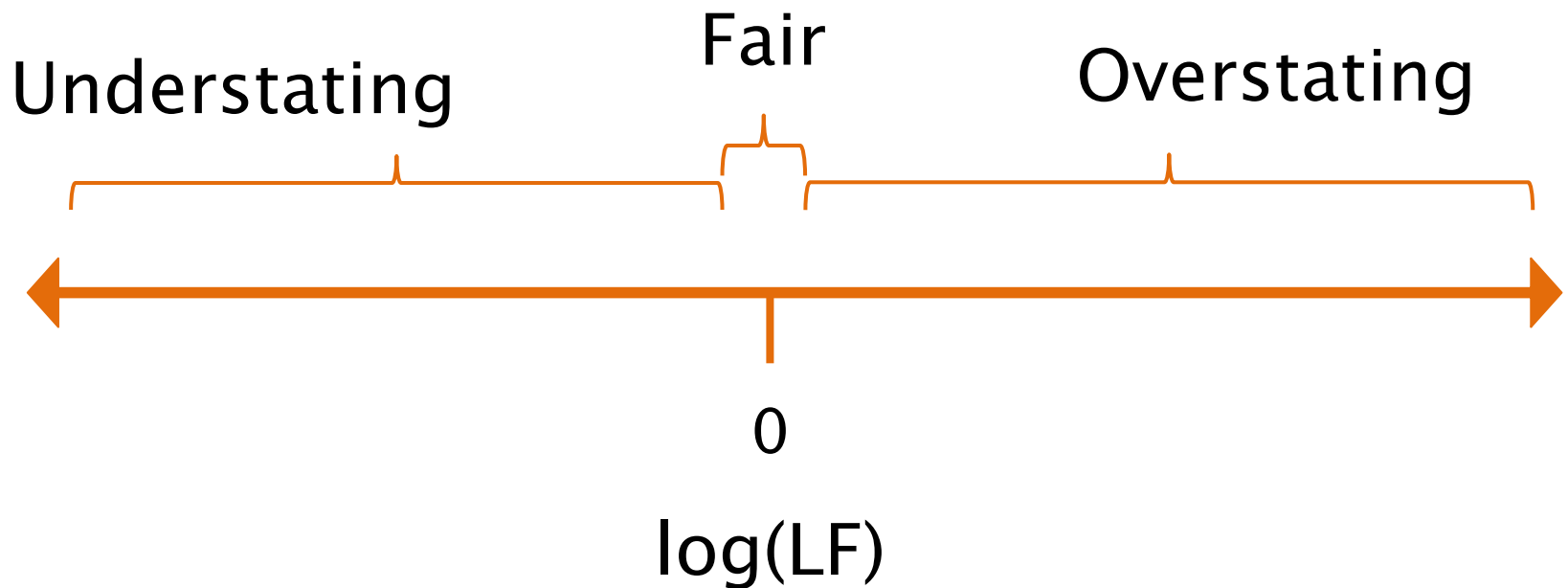
Lie Factor

$$LF = \frac{\text{size of effect shown in graphic}}{\text{size of effect in data}}$$



Lie Factor

$$LF = \frac{\text{size of effect shown in graphic}}{\text{size of effect in data}}$$



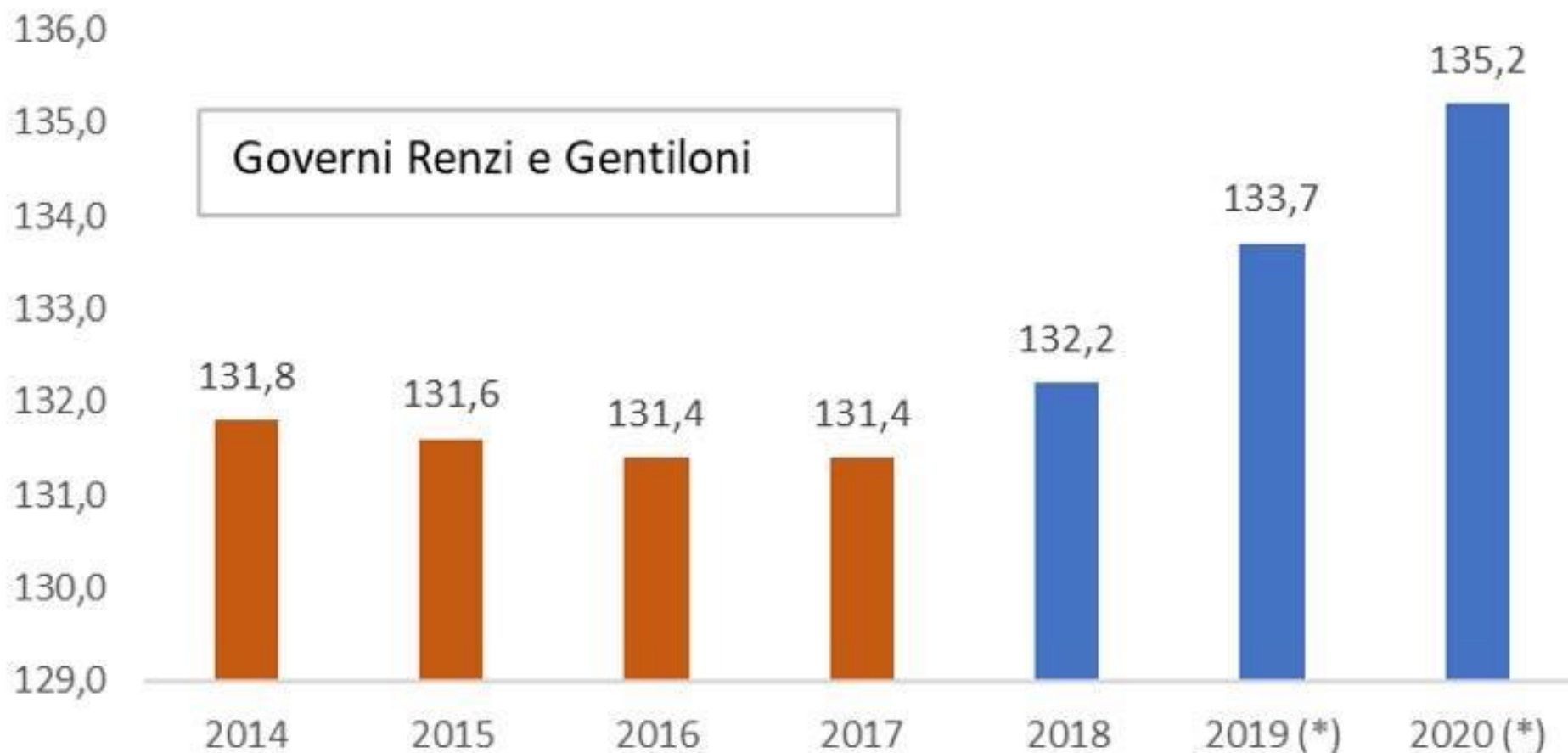
Lie Factor – Example

Debito pubblico (% PIL)

(*) previsioni Commissione UE

Governo Conte

Governi Renzi e Gentiloni

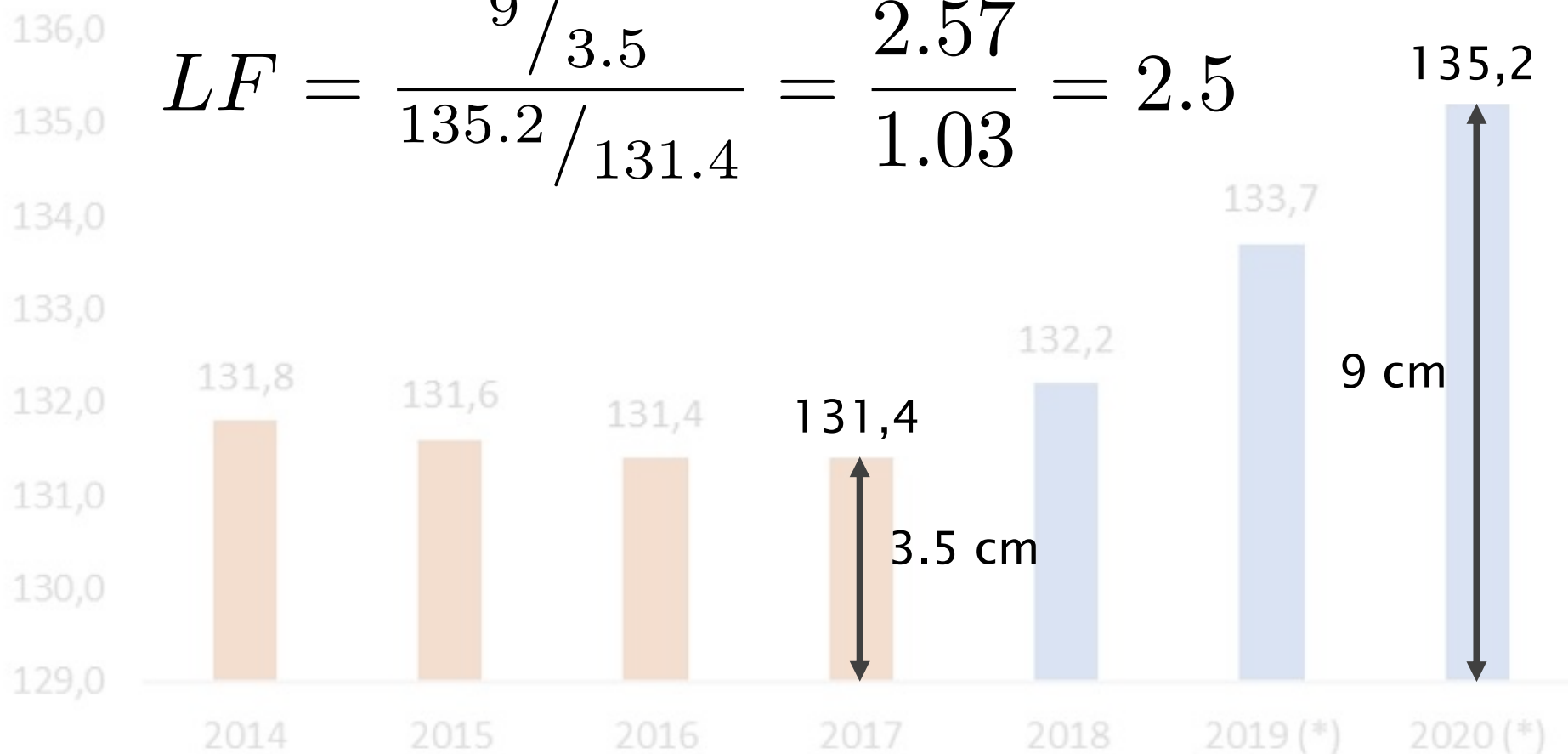


Lie Factor – Example

Debito pubblico (% PIL)

(*) previsioni Commissione UE

$$LF = \frac{9 / 3.5}{135.2 / 131.4} = \frac{2.57}{1.03} = 2.5$$

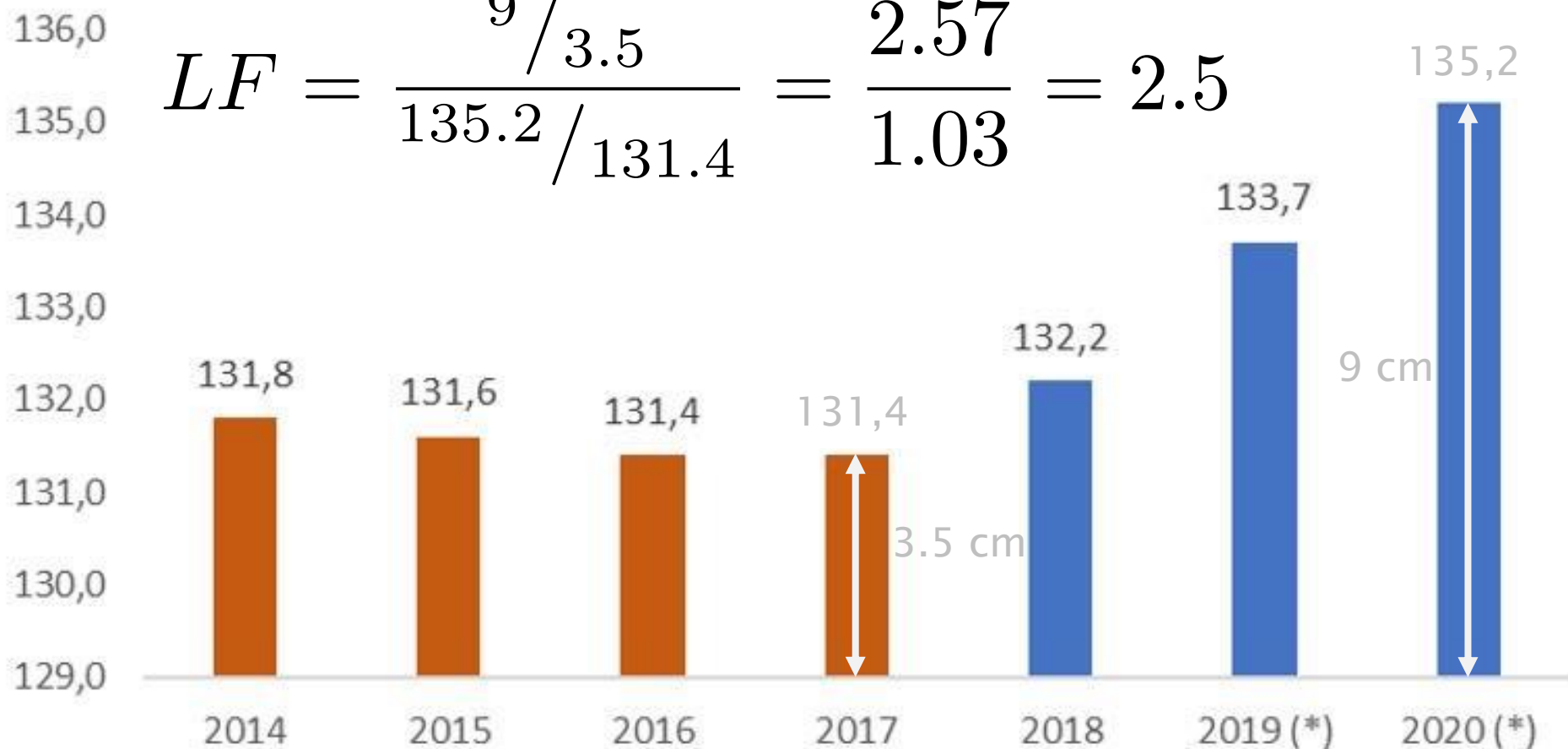


Lie Factor – Example

Debito pubblico (% PIL)

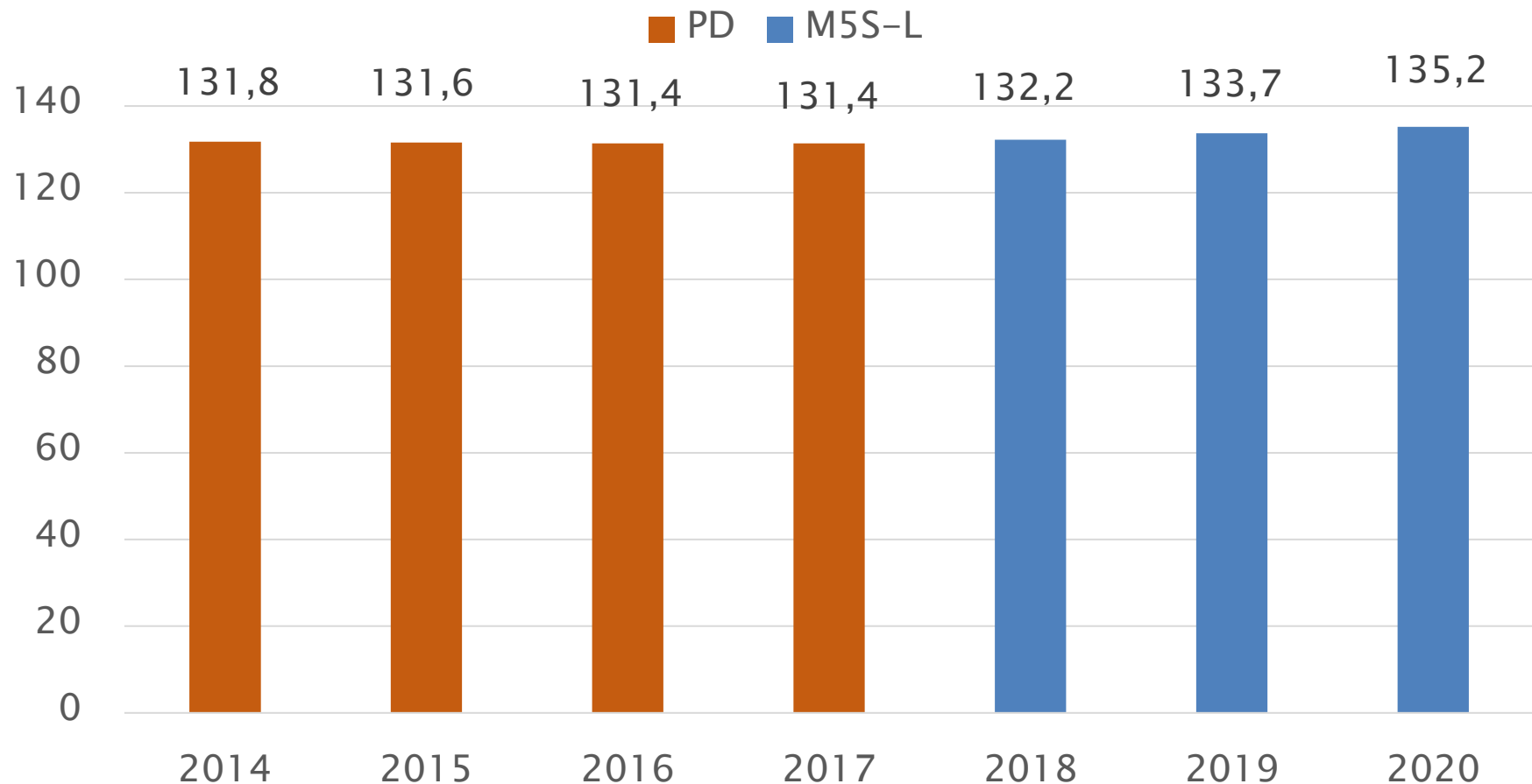
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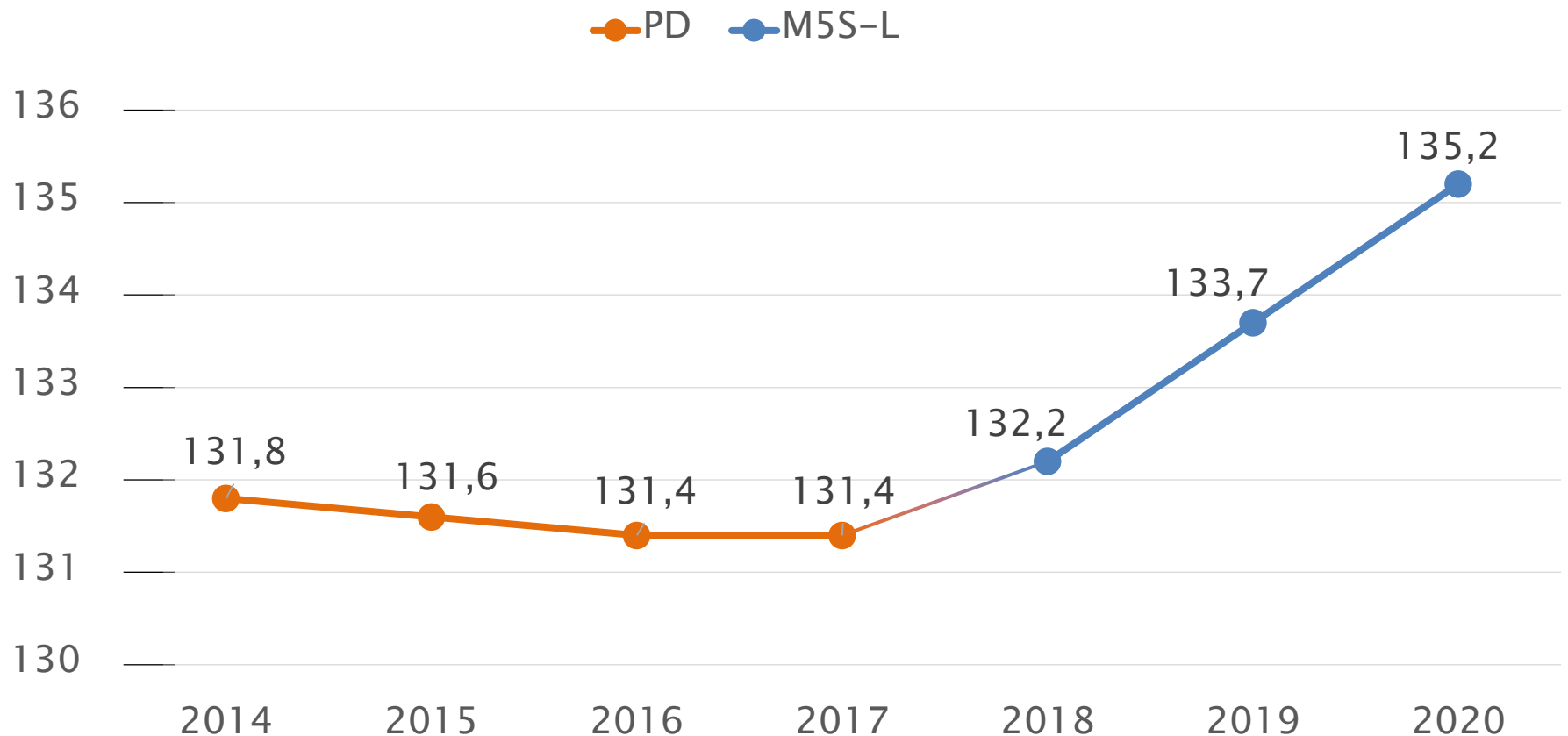
Lie Factor –Redesign

Debito Pubblico (% PIL)



Lie Factor – Redesign

Debito Pubblico (% PIL)



Guidelines for design

- Keep the physical Lie Factor = 1
- Limit the perceptual Lie Factor as much as possible
 - ◆ Per Steven's law, avoid area comparisons

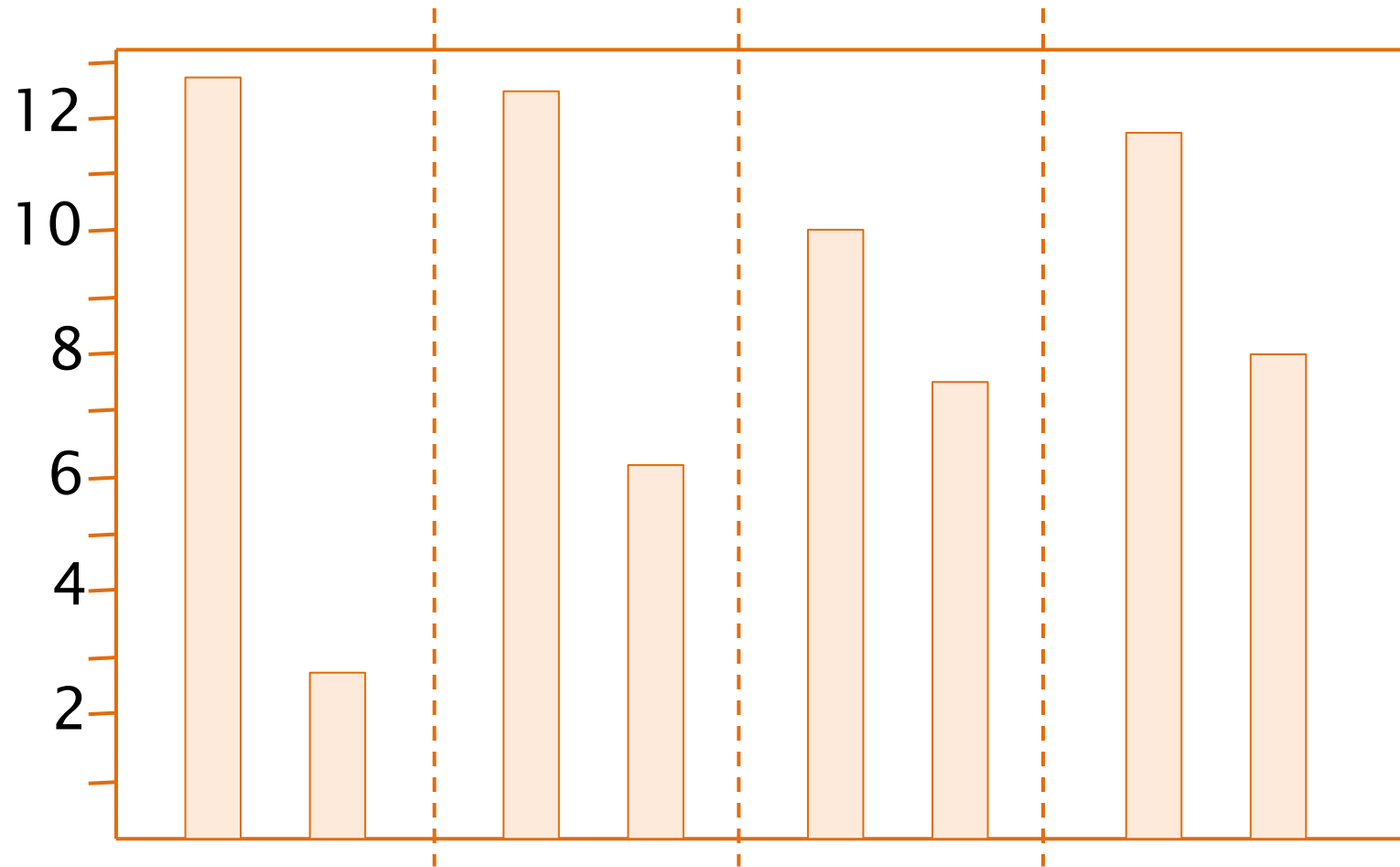
- Every element should convey useful information
- Unnecessary visual objects or attributes distract from the message
 - ◆ Different attributes trigger a search for a rationale (e.g. random colors)

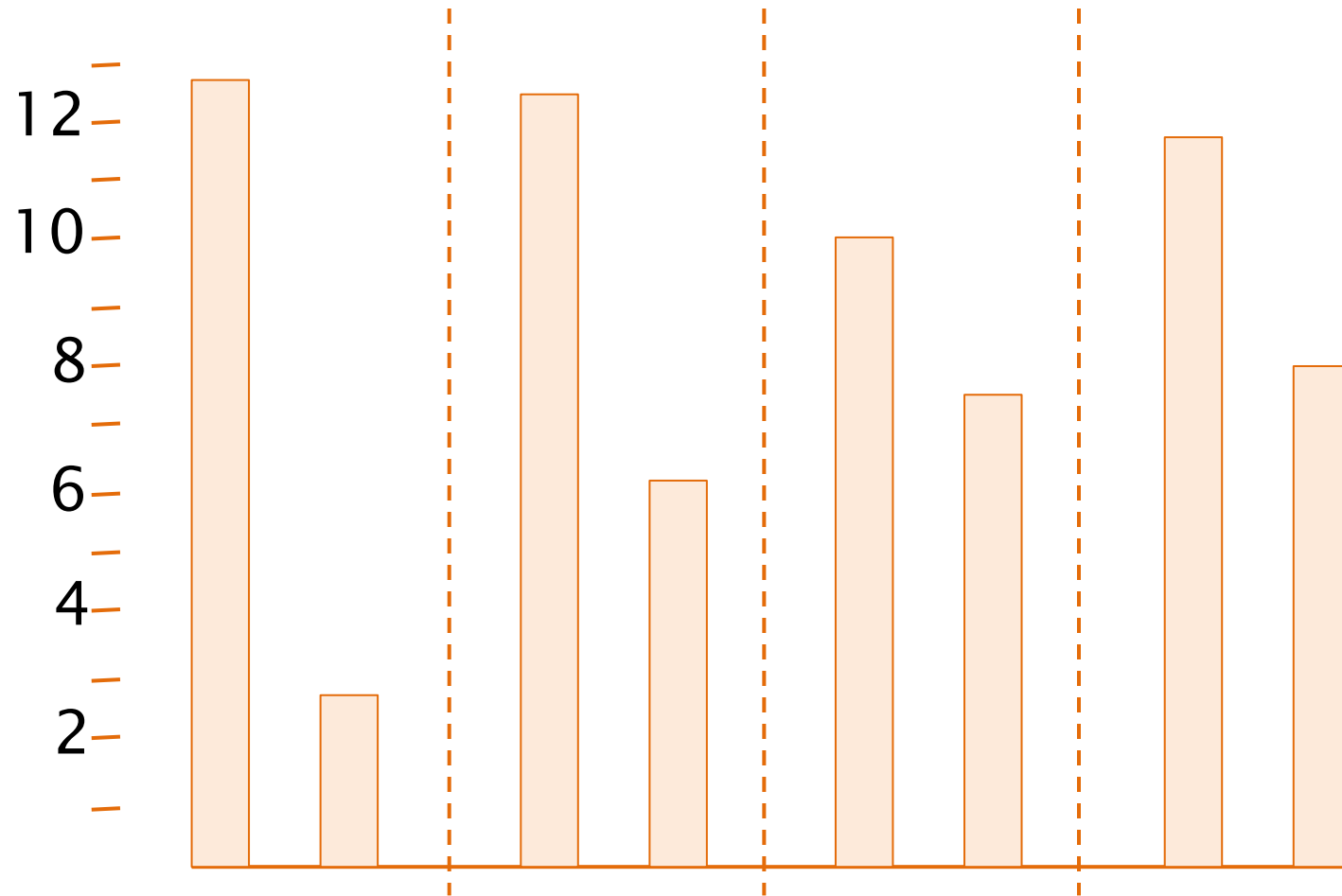
$$\text{Data-ink ratio} = \frac{\text{data ink}}{\text{total ink used to print the graphic}}$$

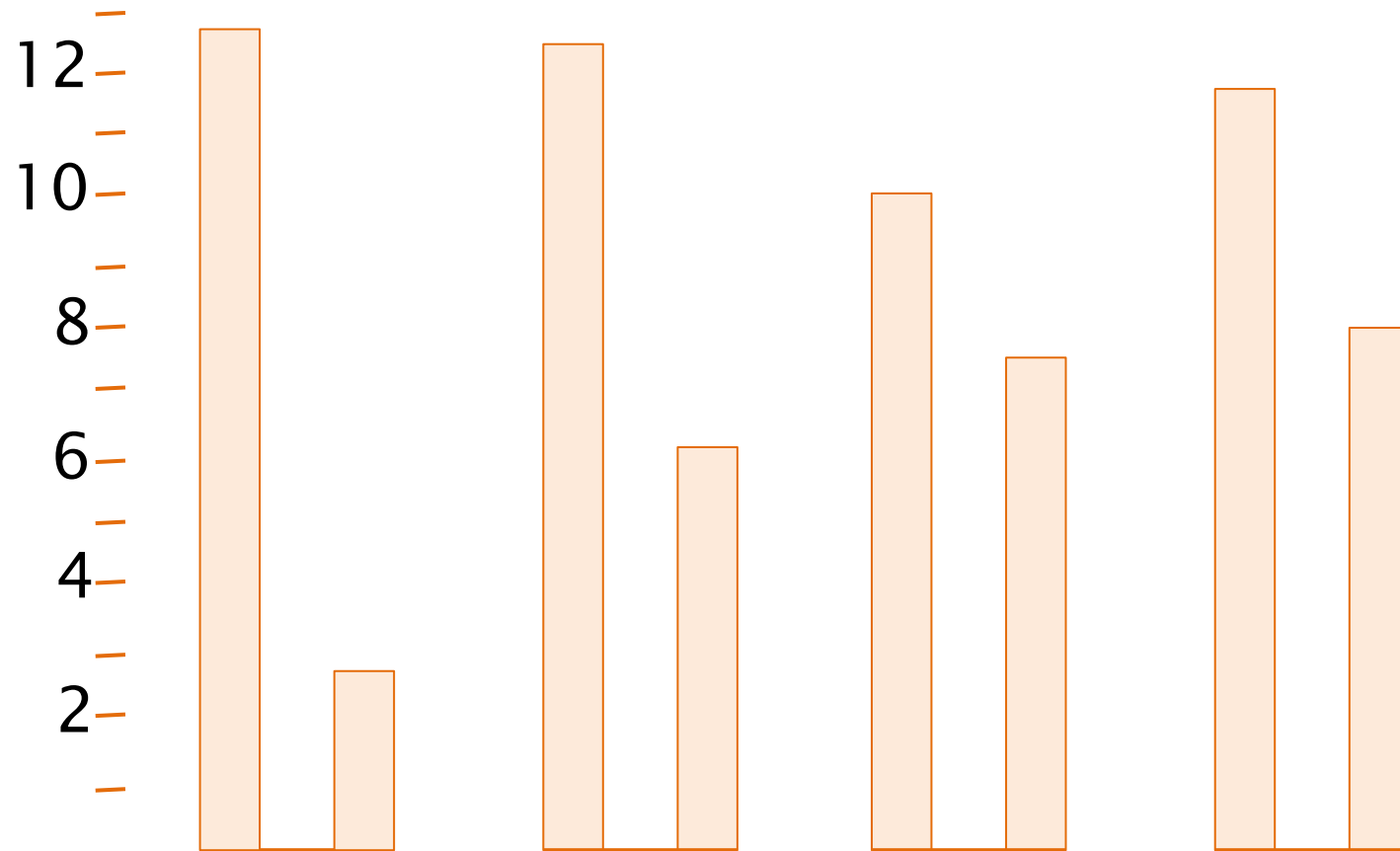
- Proportion of a graphic's ink devoted to the non-redundant display of data information

◆ Or:

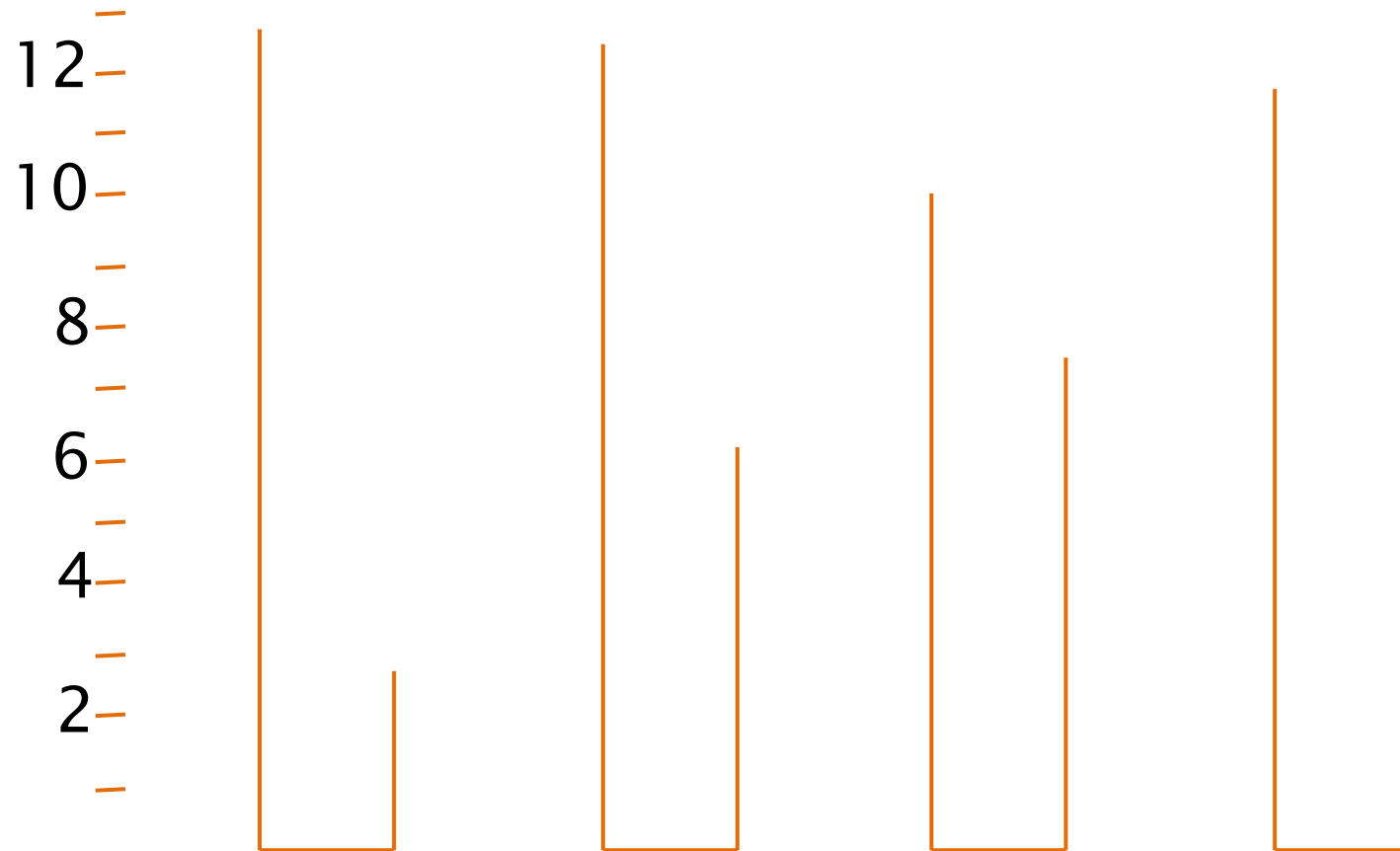
$$1 - \frac{\text{ink that can be erased without loss of information}}{\text{total ink used to print the graphic}}$$







Data-ink



Tufte's proposed redesign

Guidelines for design

- Maximize data–ink ratio
 - ◆ Erase non–data–ink
 - ◆ Erase redundant data–ink
- “Within reason”

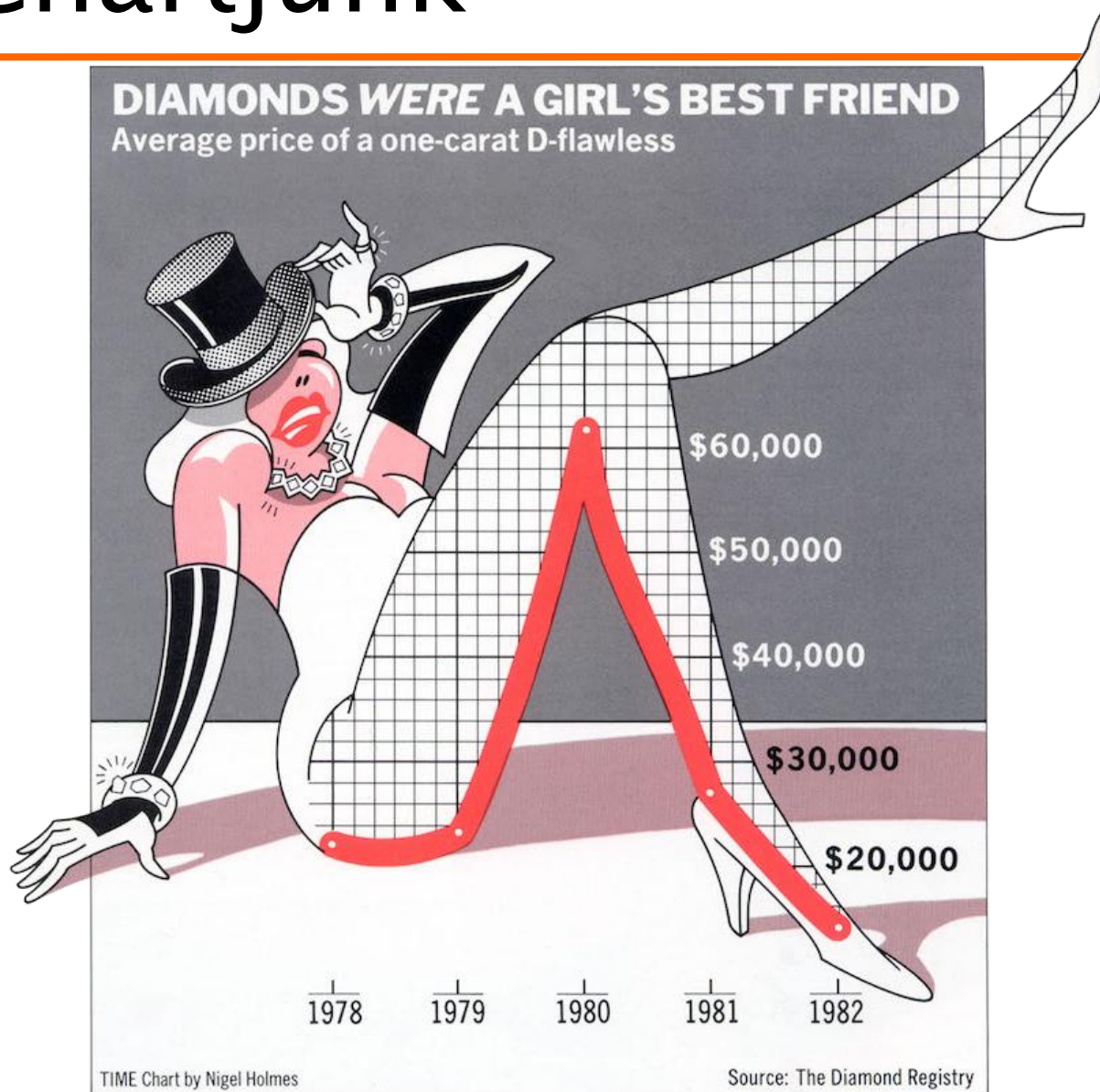
Above all else show the data
E. Tufte

Use of contrast

- Include differences corresponding to actual differences
- Effective when one item is different in a context of other items that are the same
 - ◆ Bright saturated color among mid colors

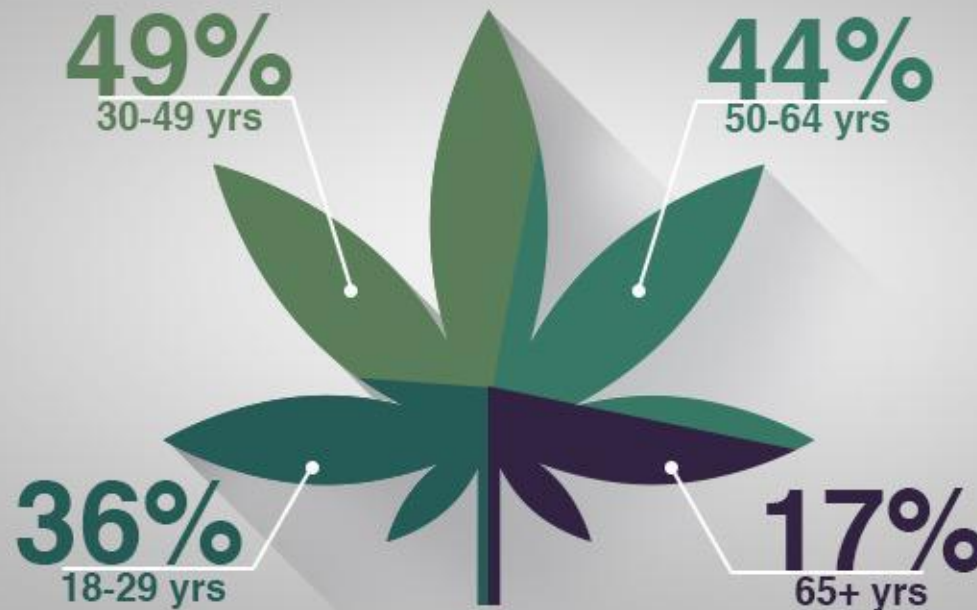
- The presence of unnecessary elements that distract or hide the message conveyed by the diagram

Chartjunk



Nigel Holmes:
<http://nigelholmes.com>

AMERICANS WHO HAVE TRIED WEED



Source: Gallup



SUNDAYS
10^P
ET/PT

#highprofits

- Visual encoding and layout should make perception tasks easy and effortless
- Textual and support elements should provide effective support to understanding the information
- Any variation in the graph should represent useful information otherwise it is noise obfuscating the message

- **Textual** elements should provide effective support to understanding
 - ◆ Hierarchical
 - Size and position reflects importance
 - ◆ Readable
 - Large enough
 - ◆ Horizontal
 - ◆ Close to data (avoid legends)
- Always label the axes

- Get it right in black and white
- Use medium hues or pastels
 - ◆ Bright colors distract and tire out
- Use color only when needed to serve a particular communication goal

Cognitive Dissonance



ROSSO



BLU



VERDE



GIALLO

Efficiency and efficacy of perception tasks is affected by:

- **Detection**

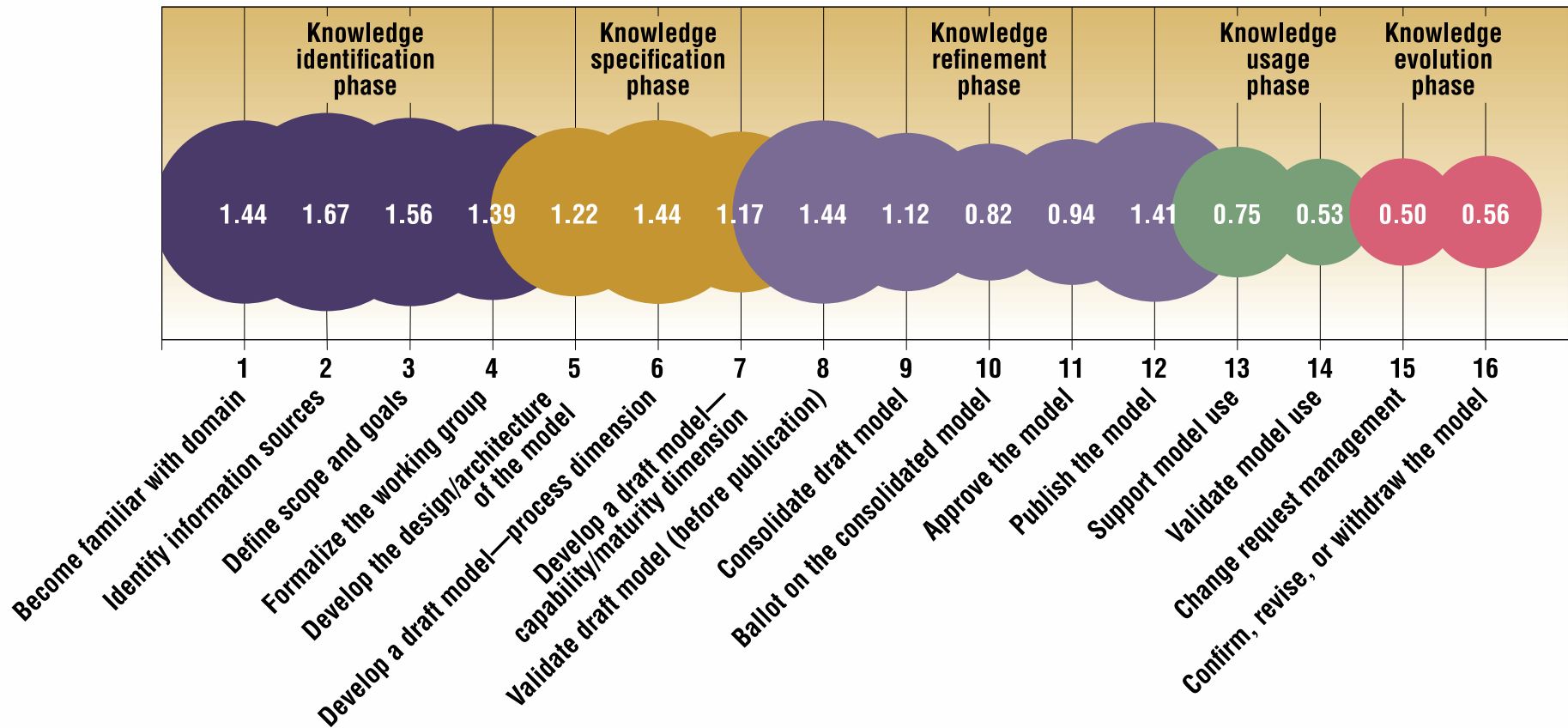
The capability to visually identify the objects that represent the data to be compared

- **Separation**

The distance between the objects to be compared

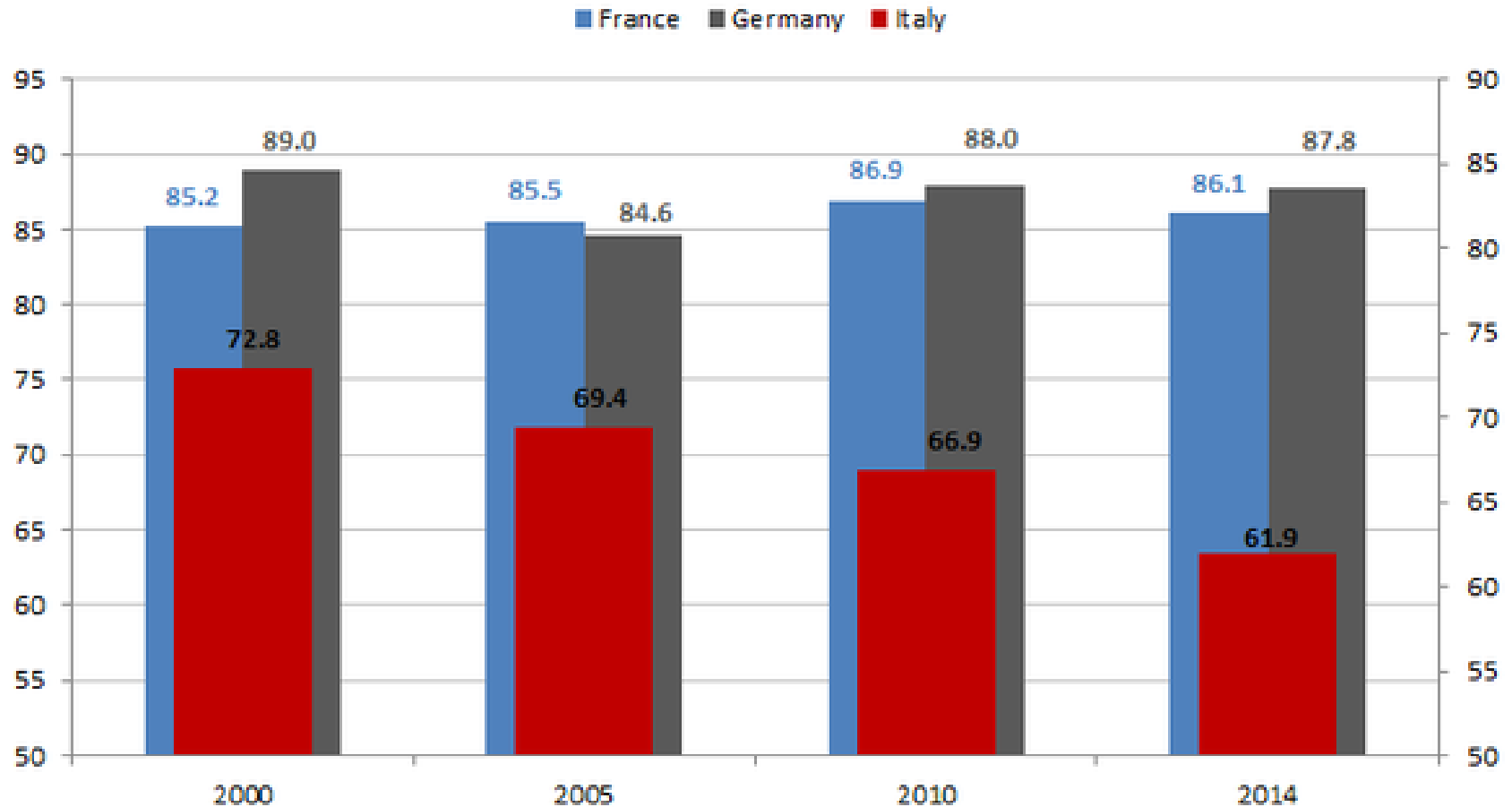
- affects negatively the accuracy

Clarity



Example

Trends in employment rates of 25-34 with a tertiary degree



Analysis

- Proportionality
 - ◆ Due to non-zero base bars, it has a large lie factor (2.2):
 - ratio of real values: 87.8 : 61.9
 - ratio on graph: 37.8 : 11.9
- Utility
 - ◆ Most elements appear useful
 - ◆ X-axis ticks can be removed
 - ◆ Y grid could be made less prominent

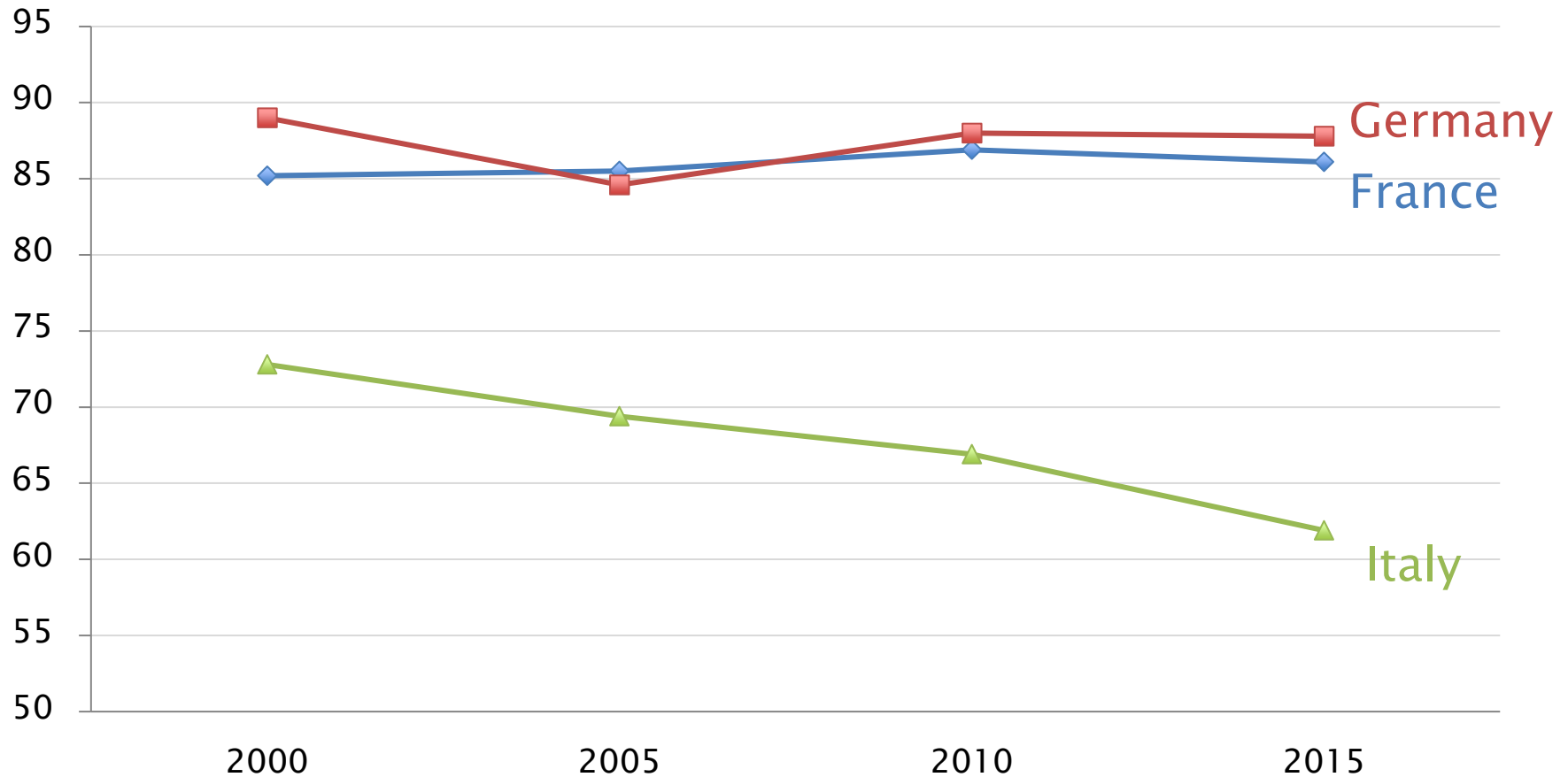
Analysis

- Clarity

- ◆ It uses a **dual scale** that confuses and makes very hard a visual comparison of the values and further distorting the compared values.
- ◆ The dual scale is not mentioned anywhere and it is not clear which values refer to which scale.
- ◆ In general the usage of bars is not the most appropriate visual representation if the goal is to show a trend or evolution in time.

Redesign

Trends in employment rates of 25–34 with a tertiary degree



References

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 - ♦ http://www.perceptualedge.com/articles/visual_business_intelligence/rules_for_using_color.pdf
- D. Borland and R. M. Taylor II, "Rainbow Color Map (Still) Considered Harmful," in *IEEE Computer Graphics and Applications*, vol. 27, no. 2, pp. 14–17, March–April 2007.
 - ♦ http://ieeexplore.ieee.org/xpls/abs_all.jsp?arnumber=4118486
- <http://www.color-blindness.com>
- <http://www.csc.ncsu.edu/faculty/healey/PP/index.html>